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AN ATLAS OF SOLAR FLARE EFFECTS OBSERVED ON LONG VLF PATHS DURING 1961

C. J. CHILTON, F. K. STEELE, AND D. D. CROMBIE



**U. S. DEPARTMENT OF COMMERCE
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Boulder, Colorado

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AN ATLAS OF SOLAR FLARE EFFECTS OBSERVED ON LONG VLF PATHS DURING 1961

C. J. Chilton, F. K. Steele, and D. D. Crombie

Effects produced by 37 solar flares
on four long VLF paths during 1961 are
shown and tabulated.

1. Introduction

Since early in 1961, the phase and amplitude of various very-low-frequency transmissions have been monitored by the Boulder Laboratories of the National Bureau of Standards; the NBS field site at Maui, Hawaii; the Battelle Research Institute, Frankfurt, Germany; and the Geophysical Institute, College, Alaska. Observations of three phase-stabilized VLF transmissions over four long propagation paths were made at the above receiving sites using the VLF signals radiated from NBA(18 kc/s), Balboa, Panama; NPG(18.6 kc/s), Seattle, Washington; and GBR(16 kc/s), Rugby, England. The propagation paths, their respective lengths and geographic orientations are shown in figure 1. This VLF transmission network samples the variations occurring over approximately one quarter of the earth's surface and thus provides an excellent means for studying the effects of solar flare produced ionization over a large area of the ionosphere [Chilton, et al., 1963], as well as the normal day-to-night variation in ionospheric height.

Of the known perturbations which are observed in the recorded phase of a VLF transmission, the most easily recognizable are the Sudden Phase Anomalies (SPA's) [Bracewell and Straker, 1949], which are known to be produced by ionizing radiations emitted from the sun's chromosphere. These chromospheric flares, usually referred to as solar flares, are short-lived sudden increases in light intensity generally observed near sunspots. Optical observations show that almost all flares follow the same pattern, a rapid rise to peak intensity followed by a short period of peak intensity and a slow return to the pre-flare conditions. Typical flares have an onset time that varies from 1 to 30 minutes and the return to normal requires about 30 minutes to 2 or 3 hours. In order to provide a measure of their relative magnitude, flares have been divided into classes of importance (1, 2, 3 and 3+) according to their area and brightness. The surface area of Class 1 flares is on the order of 10^{-4} of the solar hemisphere, corresponding to a diameter of about 10^9 cm. The brightness factor is obtained by photometrically observing the H α line of the solar spectrum. The magnitude of the associated phase advance is apparently closely related to the increase in solar radiation, its energy spectrum, its angle of incidence at the lower regions of the ionosphere, and to the length of path over which a lowering of the apparent height of reflection occurs.

It is the sole purpose of this note to provide examples of the solar flare effects observed on the paths listed above during 1961. Emphasis has been placed on those flares for which observations are available on more than one path.

2. Experimental Observations and Description of the Data

The propagation paths are shown in figure 1. All of the paths except one (NPG-College) are sufficiently long to make it reasonable to assume that only one waveguide mode [Wait, 1962] is present. The data obtained with signals propagating along these paths show that during a solar flare the signals received over the sunlit paths exhibit sudden phase anomalies, which are not identical, either in magnitude or duration. These observations are illustrated in figures 2 through 25. These illustrations are photographic copies of the original records obtained between May 1 and December 2, 1961. In each case the phase and amplitude traces and the directions of phase advance and amplitude increase are identified. The records shown were chosen after examining all of the recorded data. Subsequently optical observations of solar flares as listed in the CRPL Series F, Part B (Solar-Geophysical Data) Bulletins were examined and times of optical sightings were obtained and added to the figures. In addition, the Solar-Geophysical Data were examined independently and times of all Class 1 or greater flares were obtained. The VLF data were then re-examined for solar flare effects at these times. Flares for which observations on two or more paths were available are included in figures 2-25, although some other flares are included because of their proximity in time to flares for which there are two or more observations. These figures contain effects observed during 37 flares. Included in the figures are some records for which there was no visual sighting; these records are very similar to those which are associated with flares and have been included for this reason. Also included are several records for which all the paths are not totally sunlit, but which nevertheless show an appreciable effect.

The SPA's and optical classification of the associated solar flares have been listed in chronological order in table 1, which in addition contains some of the more important characteristics of the SPA's, as scaled from the figures. Following the date, the optical class and time of optical sighting are listed. The next three columns list the time of first appearance of an effect on the phase records, the time of maximum effect, and the time of return to normal. Then the size of the phase anomaly $\Delta\phi$ in degrees, and in microseconds (Δt) is listed. The latter quantity, Δt is obtained from the relation

$$\Delta t = \frac{\Delta\phi}{0.36} \cdot \frac{1}{f}$$

where f is in kc/s. The size of the phase change $\Delta\phi$ produced by a given depression Δh of the ionosphere is not particularly useful in itself since it depends on the path length and the frequency of the signal, as well as on Δh . Thus Δh is a better index of the magnitude of the solar flare effect. So in the next column, values of Δh calculated in the manner described by Wait [1959, 1961] are given for all paths except NPG - College which, as noted above, is too short to assume that only one waveguide mode is present. These values of Δh are obtained on the assumption that the flare produces a constant depression along the whole path. This of course is hardly likely, since it would be reasonable to assume that the flare would produce the greatest effects at the sub-solar point, the effects becoming smaller as the zenith angle of sun increases. This might be corrected by relating the zenith angle (χ) to the calculated value of Δh since it has been shown [Chilton, et al., 1963] that when the observed Δh obtained on the above basis is plotted semilogarithmically against $1/\overline{\cos \chi}$, (where $\overline{\cos \chi}$ is the average value of $\cos \chi$ along the propagation path), a straight line results. Thus the table contains values of average χ and average $\cos \chi$ which are listed in the last two columns.

Table 1 also contains estimates of the maximum change of ϕ and ($d\phi/dt$) observed on each path, for each flare. Observed values of $d\phi/dt$ vary from as much as $90^\circ/\text{min}$ to as little as $1^\circ/\text{min}$.

In view of the wide geographical distribution of the paths on which these observations have been made, and of the distribution in time of occurrences of the flares, it seems reasonable to regard these observations as a sample of typical flare observations which might be made on any path at any time. Therefore, the scaled data from table 1 have been separated according to the optical classification of the originating flare. Table 2 thus contains for each flare of Class 1, 2 or 3, the maximum, mean, and minimum phase shifts, together with the phase shifts exceeded by 25%, 50%, and 75% of the observations. Similarly, table 3 contains corresponding values of the rate of change of phase. It can be seen from these tables that the mean and upper quartile of both the phase change and maximum rate of change of phase increase with increasing optical classification. On the other hand, this tendency is not shown clearly by either the maximum phase change or the maximum rate of change of phase. This is possibly because the change in height of the D region is related to the solar zenith angle [Chilton, et al., 1963].

3. Acknowledgments

The observations at College were made under the supervision of Dr. H. F. Bates at the Geophysical Institute, University of Alaska. Those at Frankfurt were made under the supervision of Dr. J. Eitzenberger of the Battelle Institute. The observations at Maui were made by Sada Katahara, while those at Boulder were under the supervision of A. H. Diede. The VLF program at Frankfurt, College, and Boulder is supported by the Advanced Research Projects Agency, Washington, D. C.

4. References

- Bracewell, R. N., and T. W. Straker (1949), The study of solar flares by means of very long radio waves, Monthly Notices, Roy. Ast. Soc. 109, 28.
- Chilton, C. J., F. K. Steele, and R. B. Norton (1963), VLF phase observations of solar flare ionization in the D region of the ionosphere, J. Geophys. Res. 68, 5421-5435.
- Wait, J. R. (Nov. 5, 1959), Diurnal change of ionospheric heights deduced from phase velocity measurements at VLF, Proc. IRE 47, 998.
- Wait, J. R. (1962), Comments on a paper by W. D. Westfall, Prediction of VLF diurnal phase changes and solar flare effect, J. Geophys. Res. 67, 916.

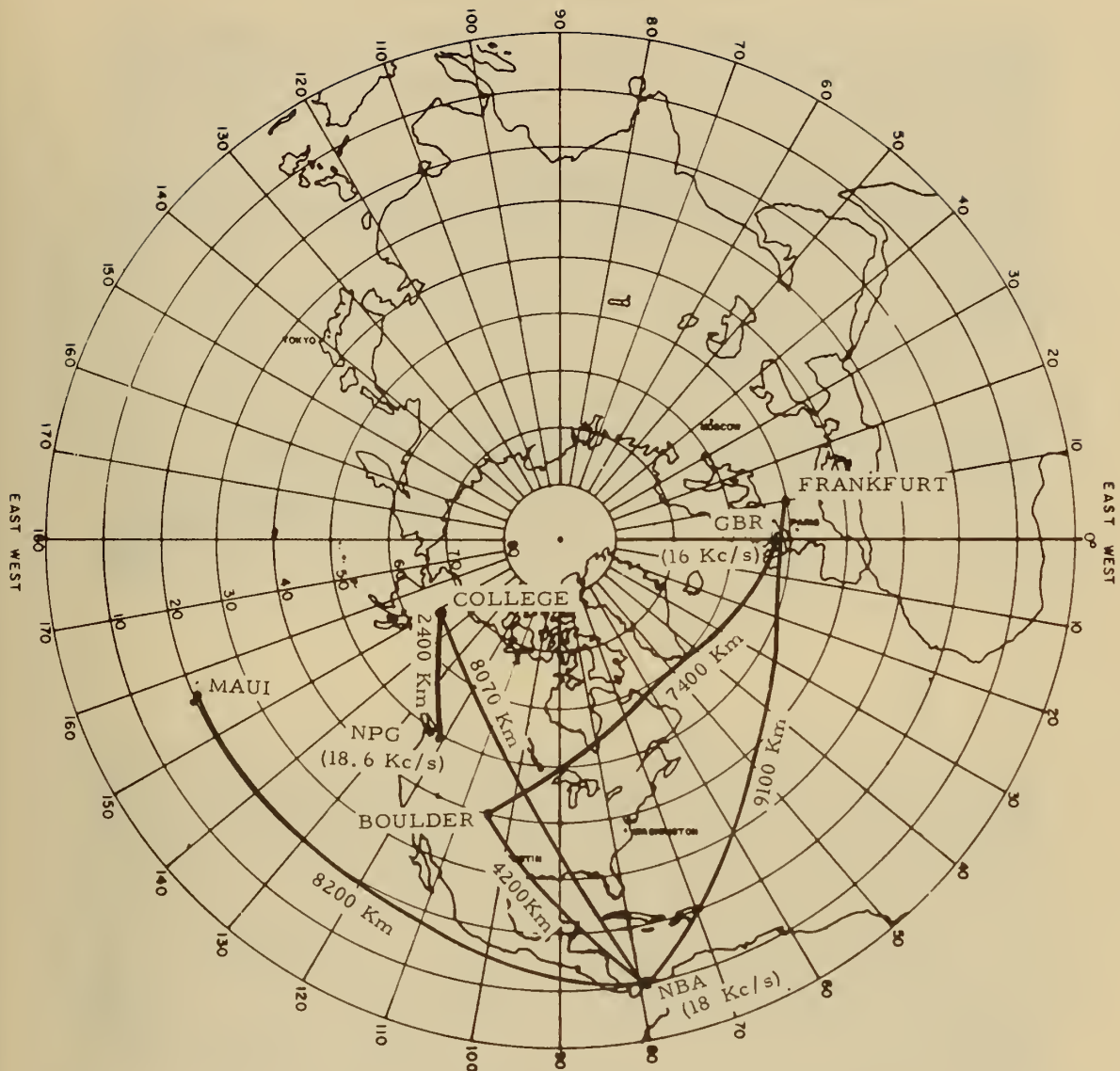


Figure 1. Map showing the paths and transmitter frequencies used in this Note.

SUDDEN PHASE ANOMALY 1 - MAY 1961 UT

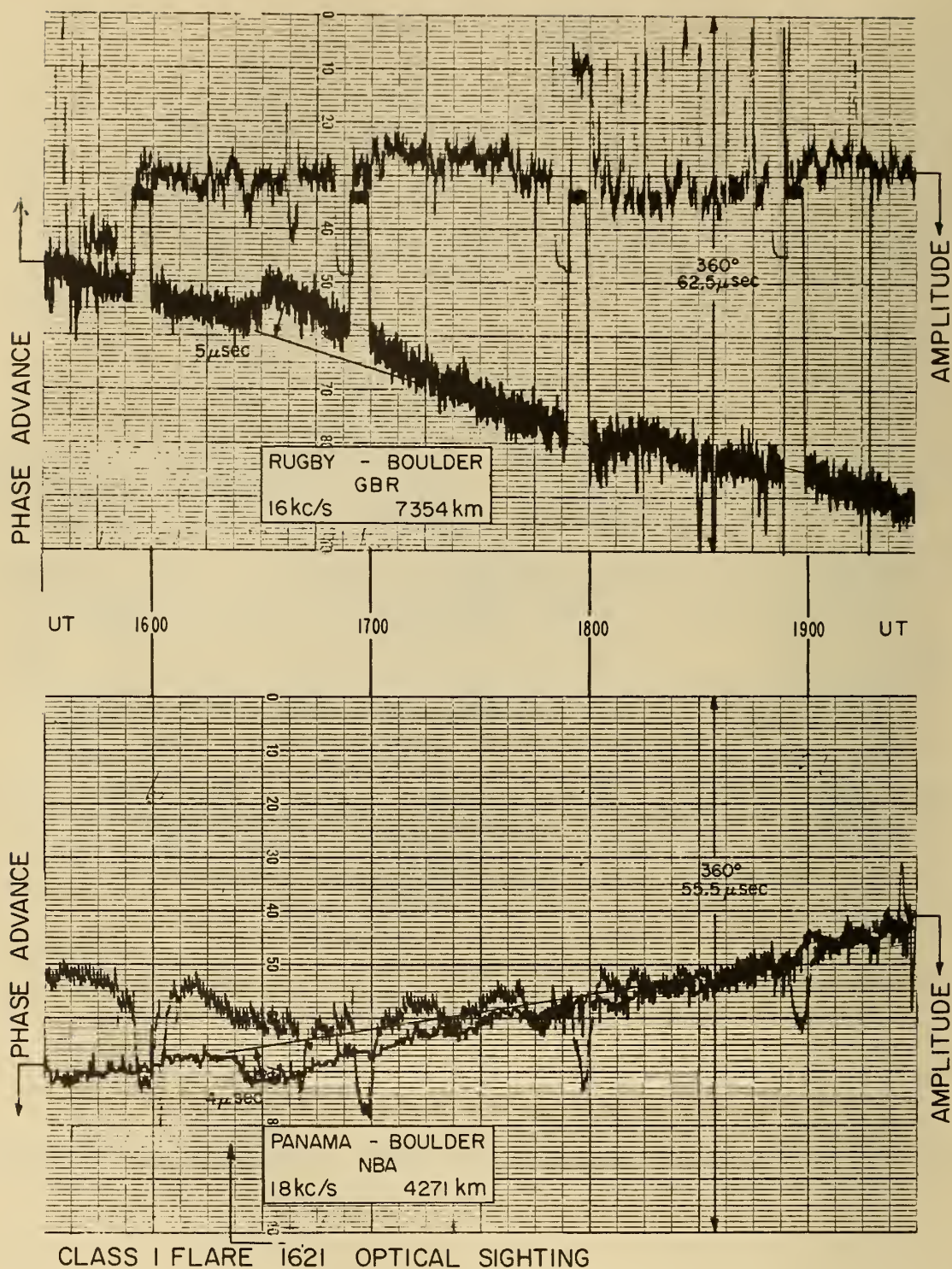


Figure 2

SUDDEN PHASE ANOMALY 5-JUNE 1961 UT

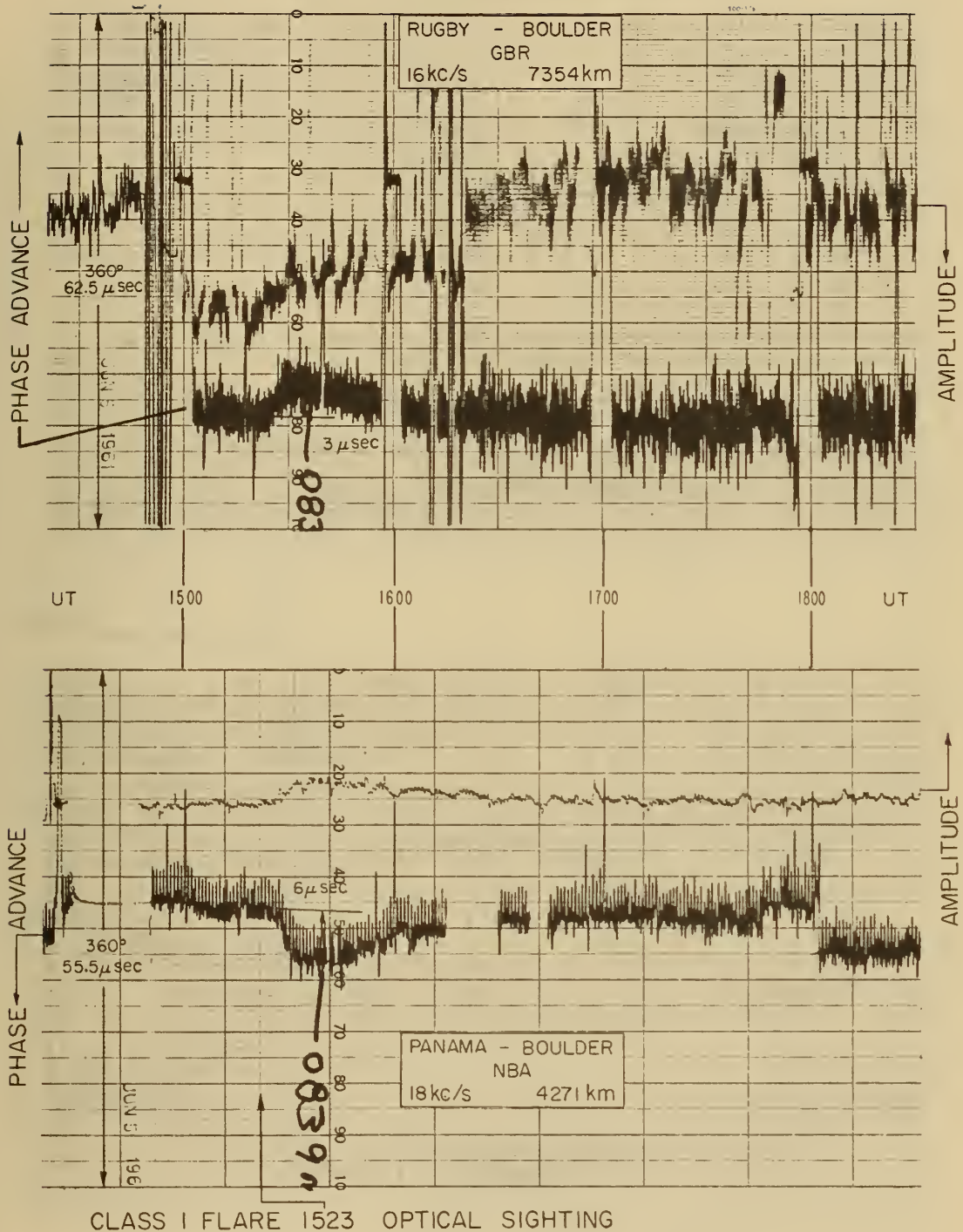


Figure 3

SUDDEN PHASE ANOMALY 11-JULY 1961 UT

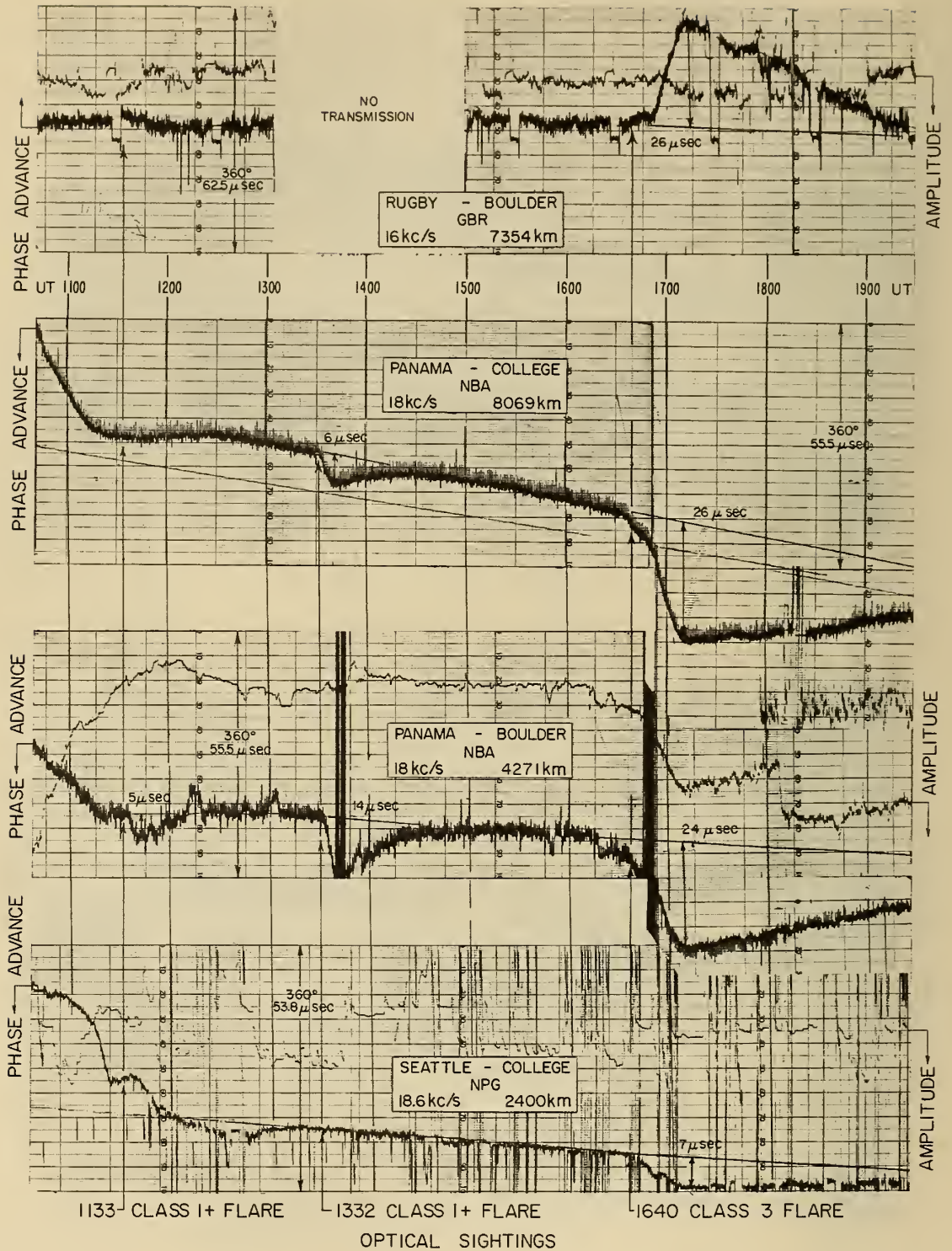


Figure 4

SUDDEN PHASE ANOMALY 15-JULY 1961 UT

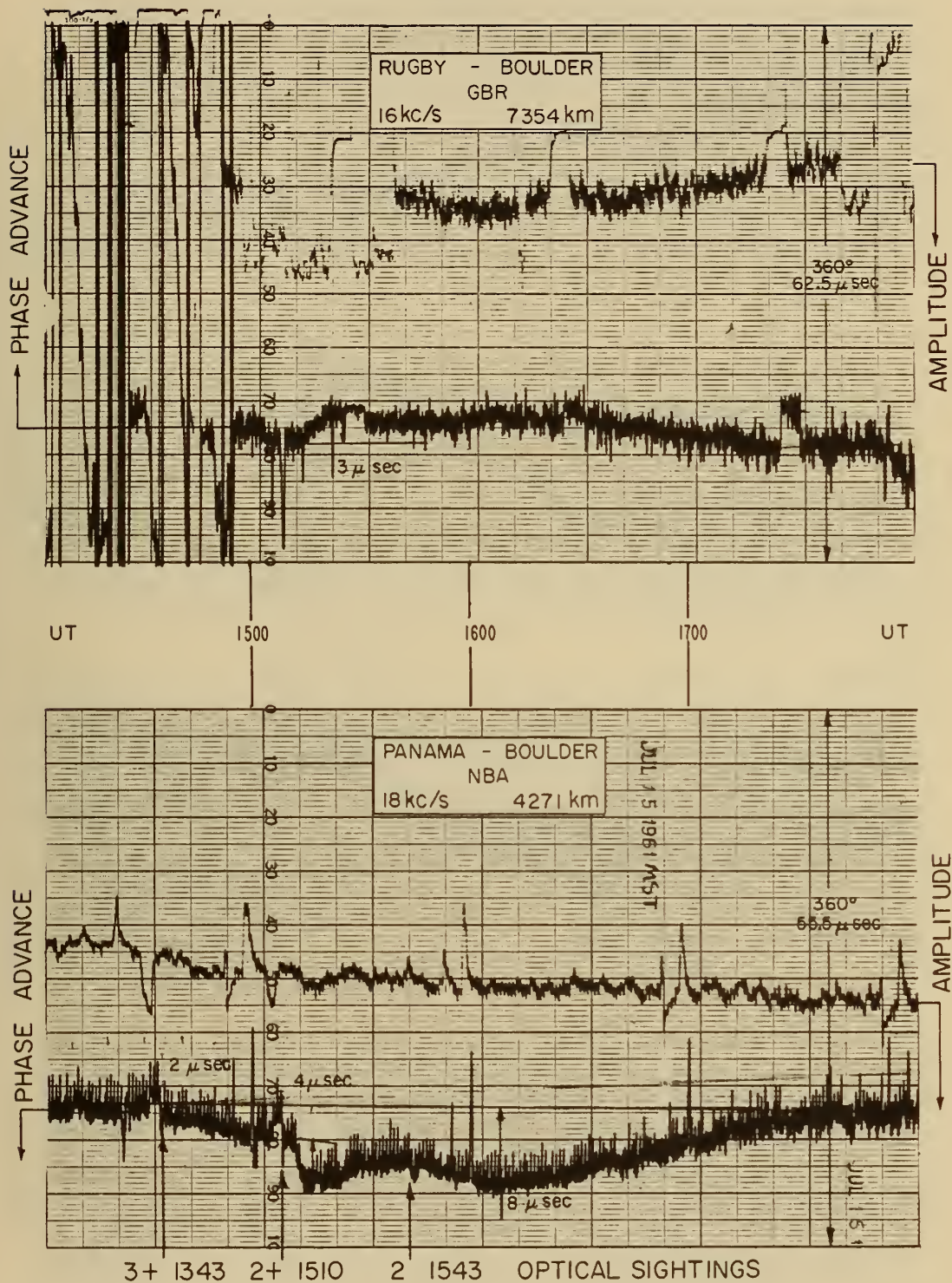


Figure 5

SUDDEN PHASE ANOMALY 17-JULY 1961 UT

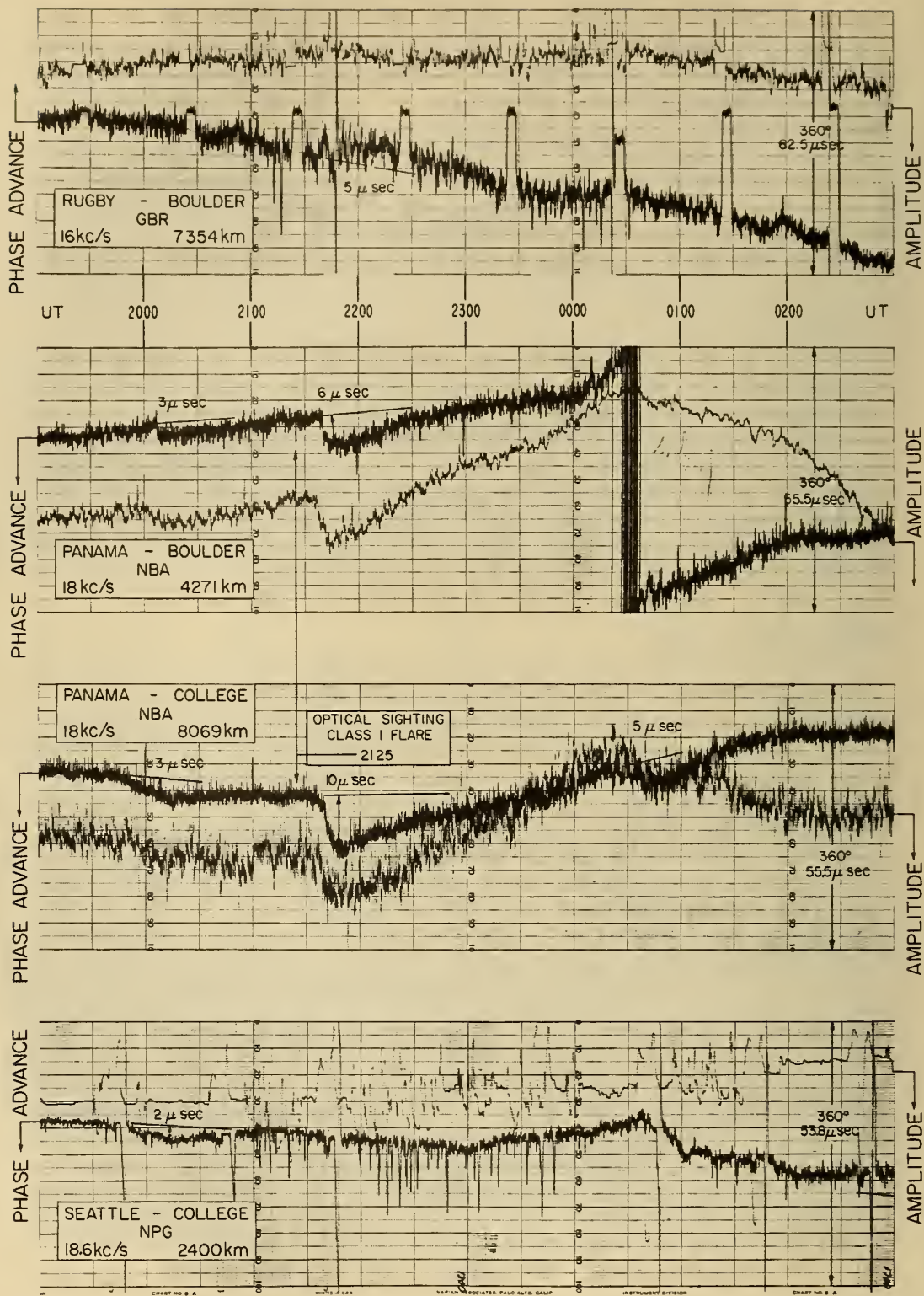


Figure 6

SUDDEN PHASE ANOMALY 18-JULY 1961 UT

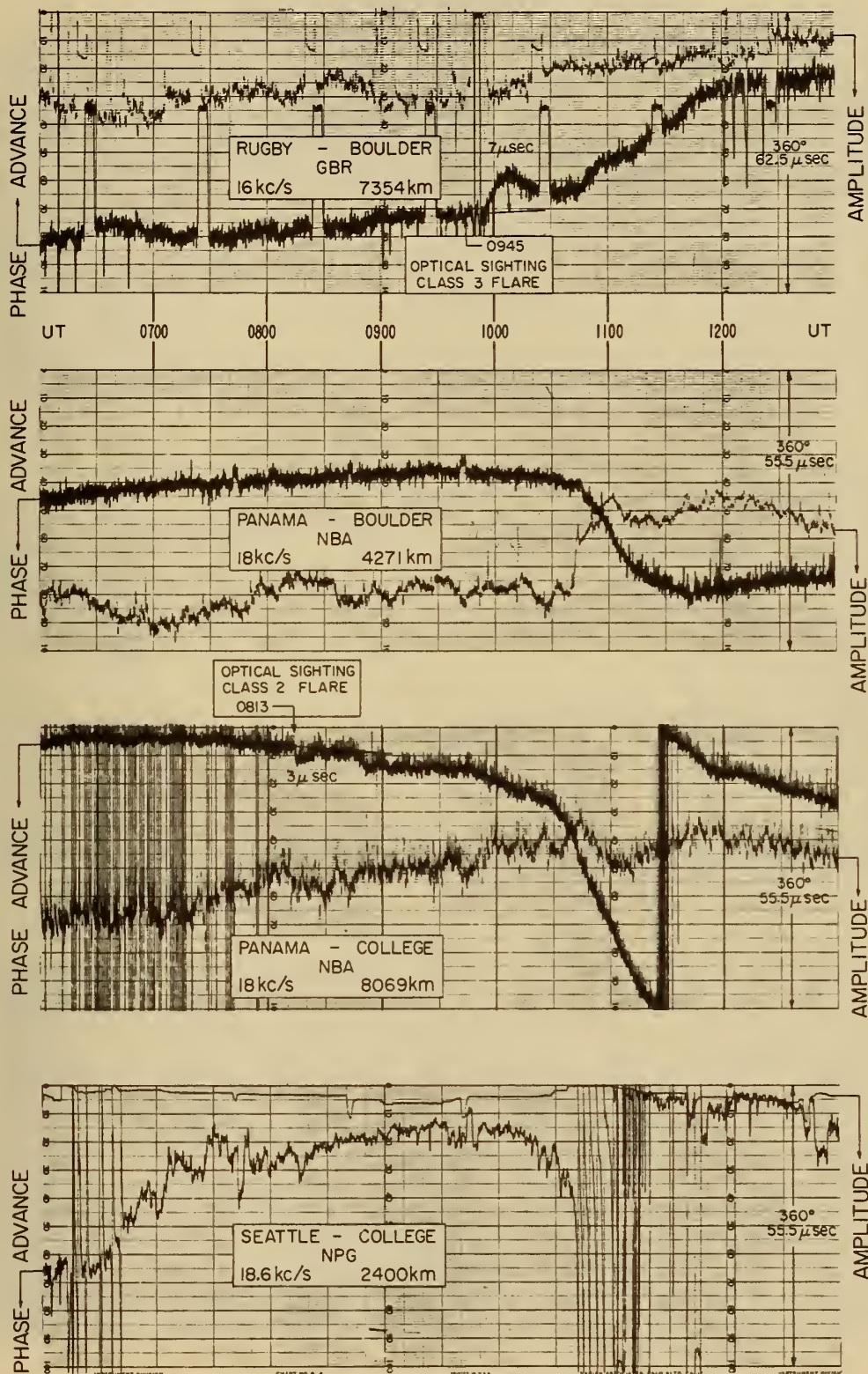


Figure 7

SUDDEN PHASE ANOMALY 20-JULY 1961 UT

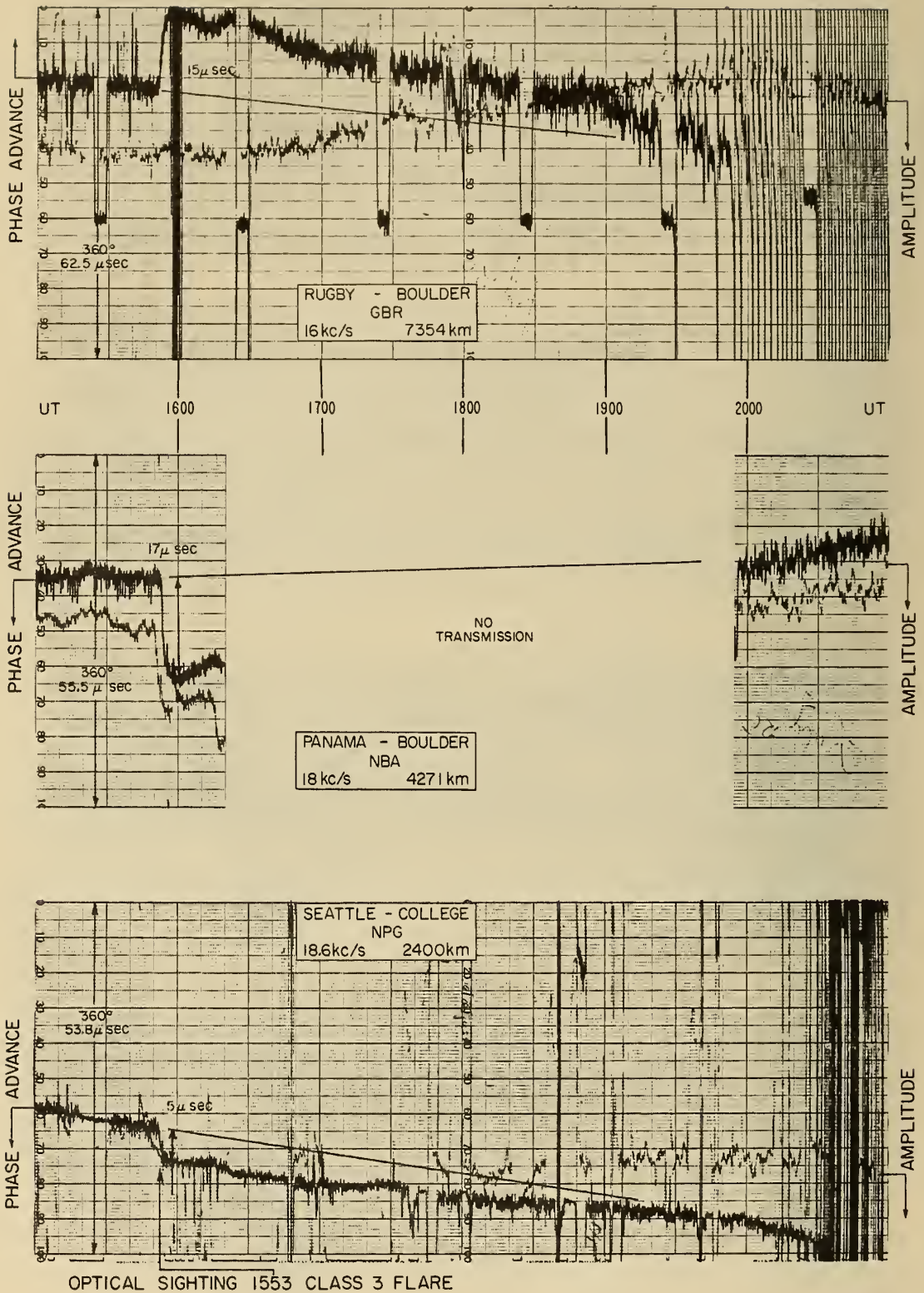


Figure 8

SUDDEN PHASE ANOMALY 21-JULY 1961 UT

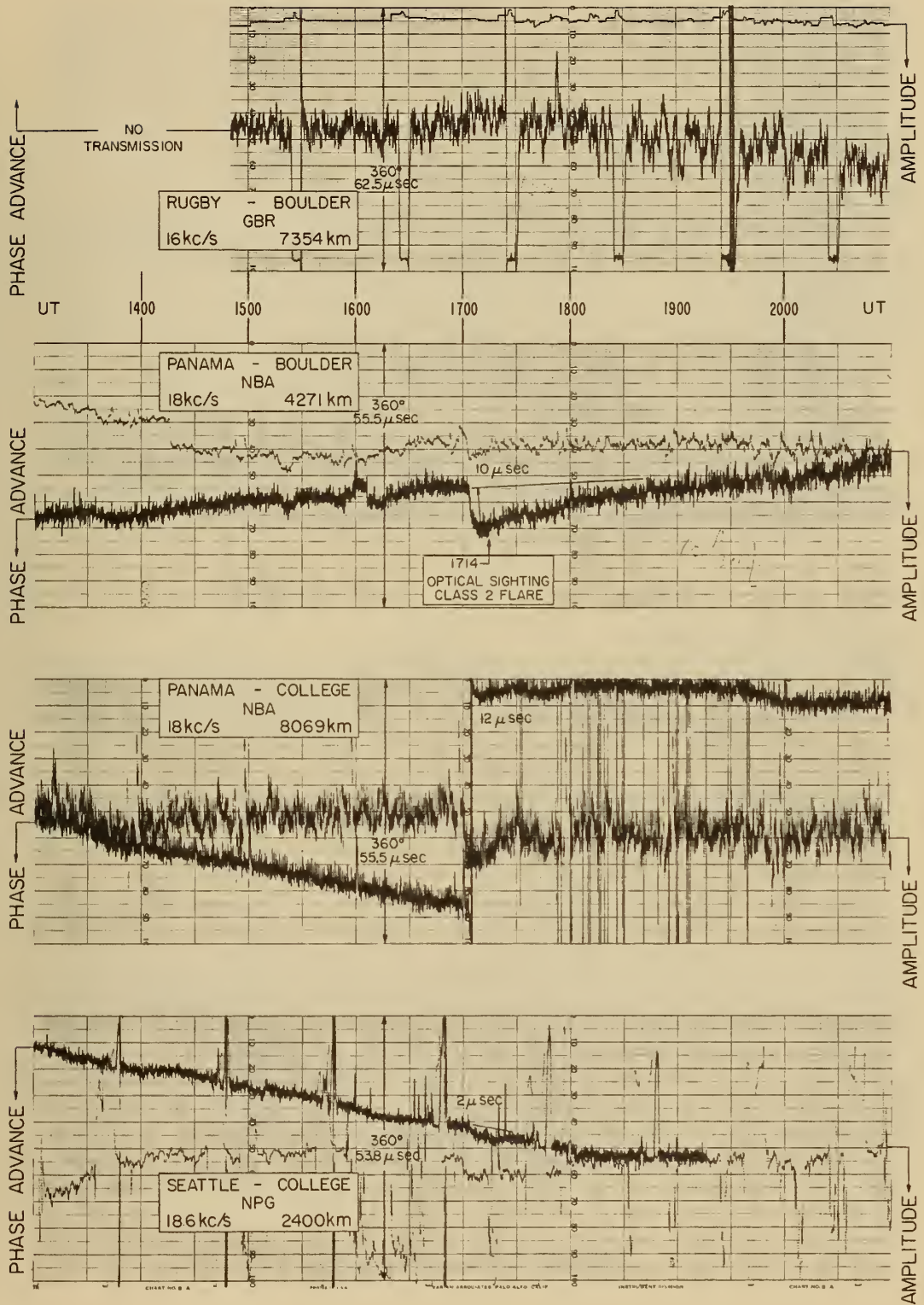
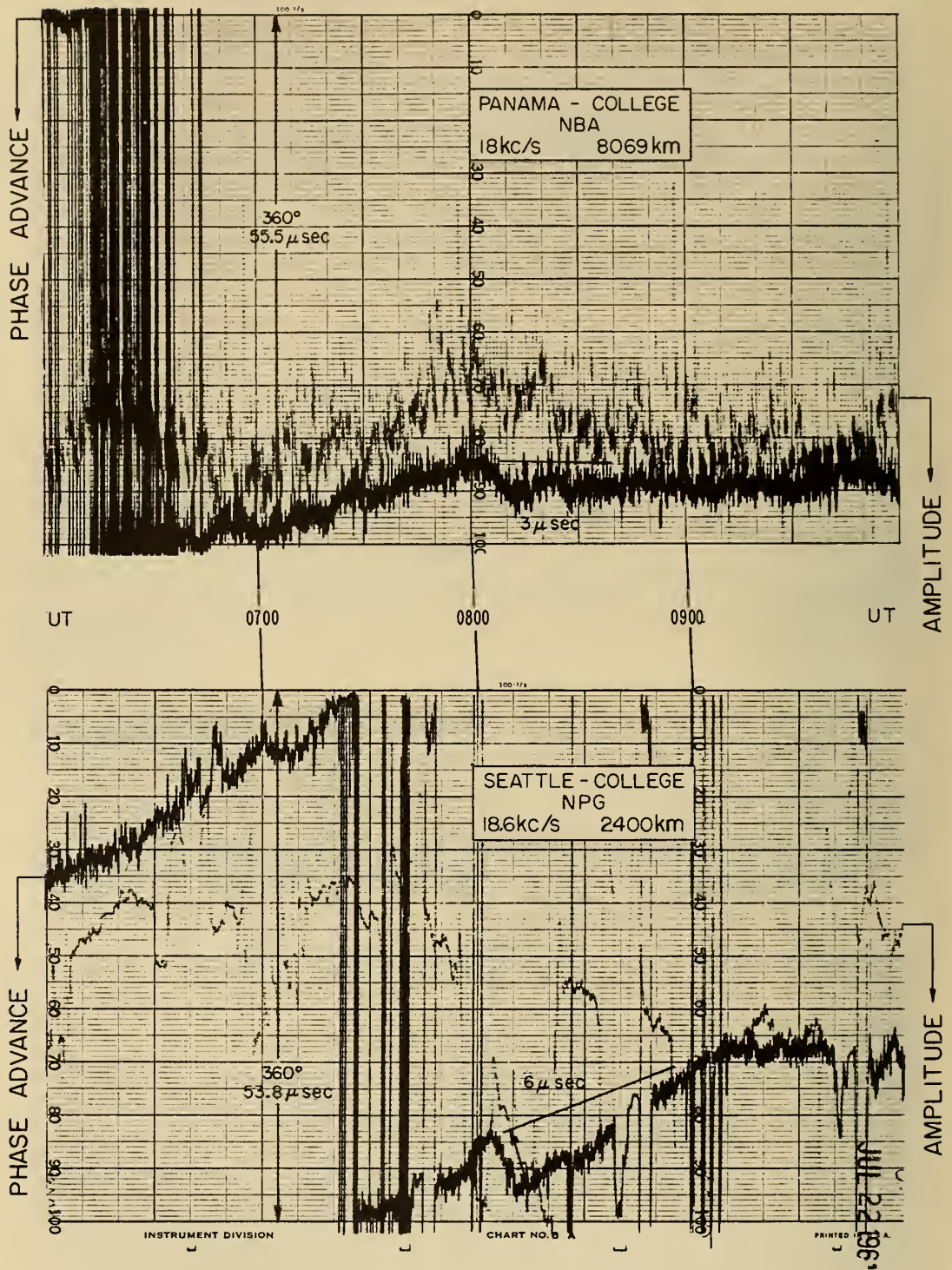


Figure 9

SUDDEN PHASE ANOMALY 23-JULY 1961 UT



NO OPTICAL SIGHTING

Figure 10

SUDDEN PHASE ANOMALY 24-JULY 1961 UT

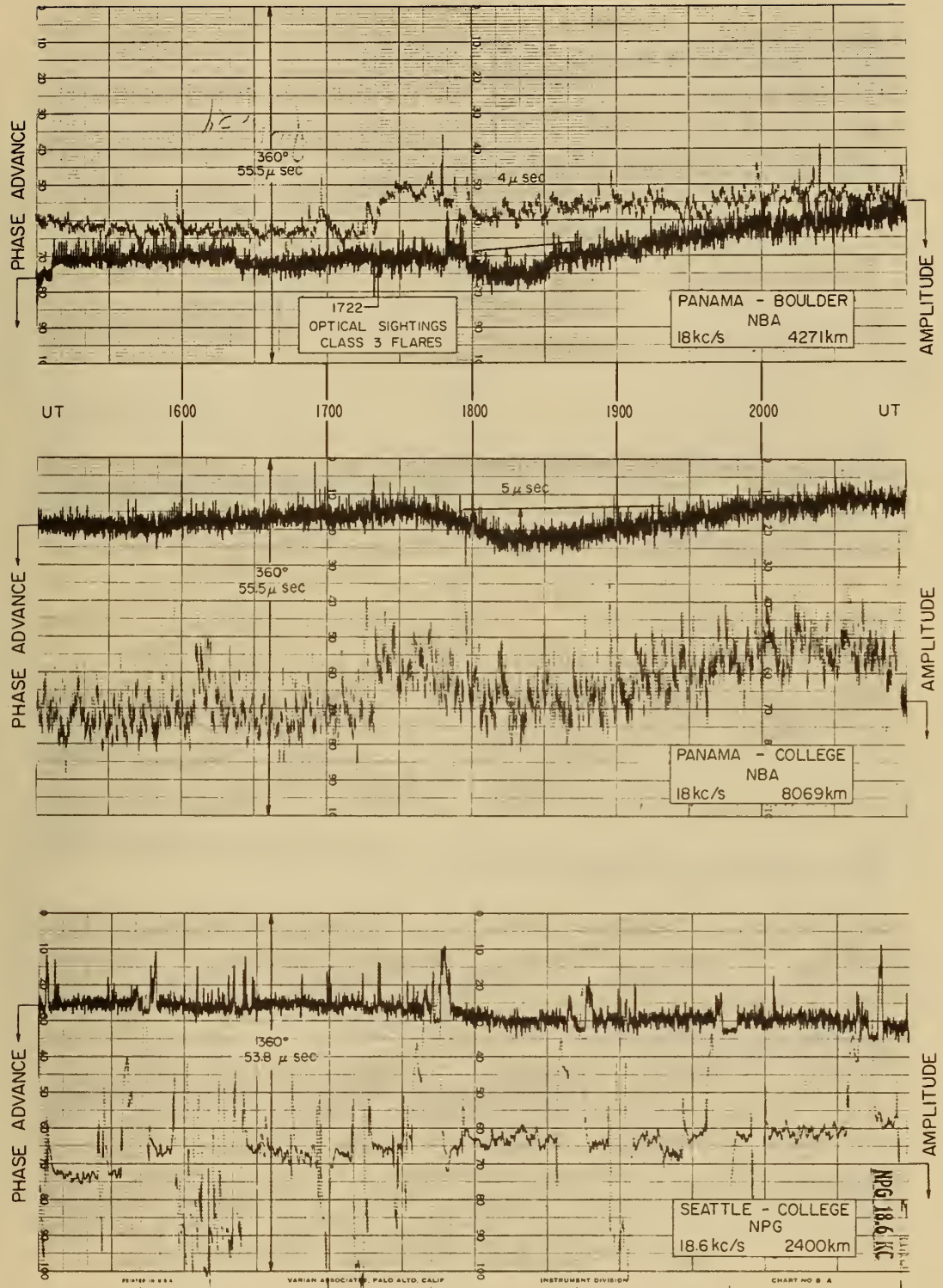


Figure 11

SUDDEN PHASE ANOMALY 15-AUGUST 1961 UT

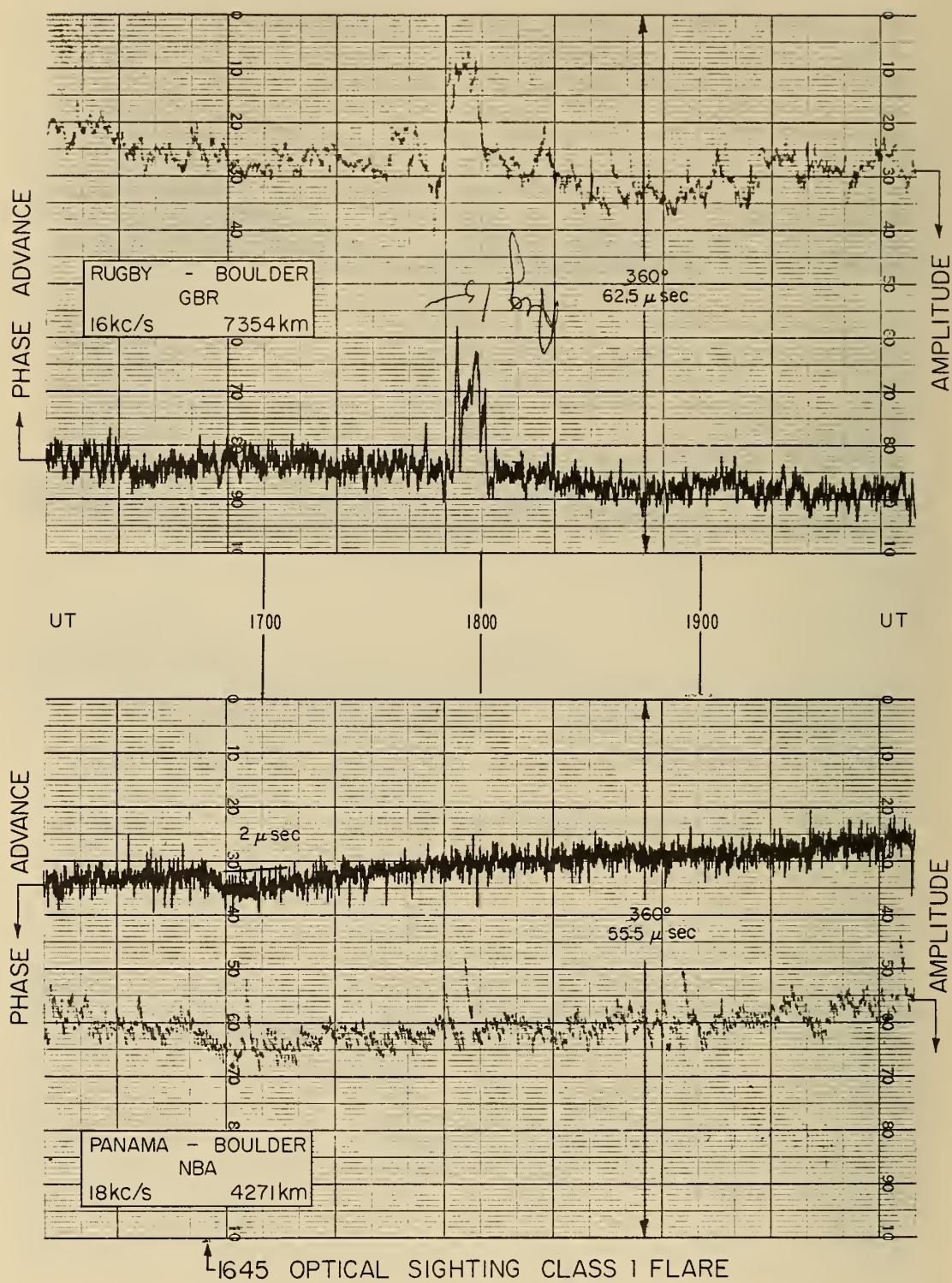


Figure 12

SUDDEN PHASE ANOMALY 18-AUGUST 1961 UT

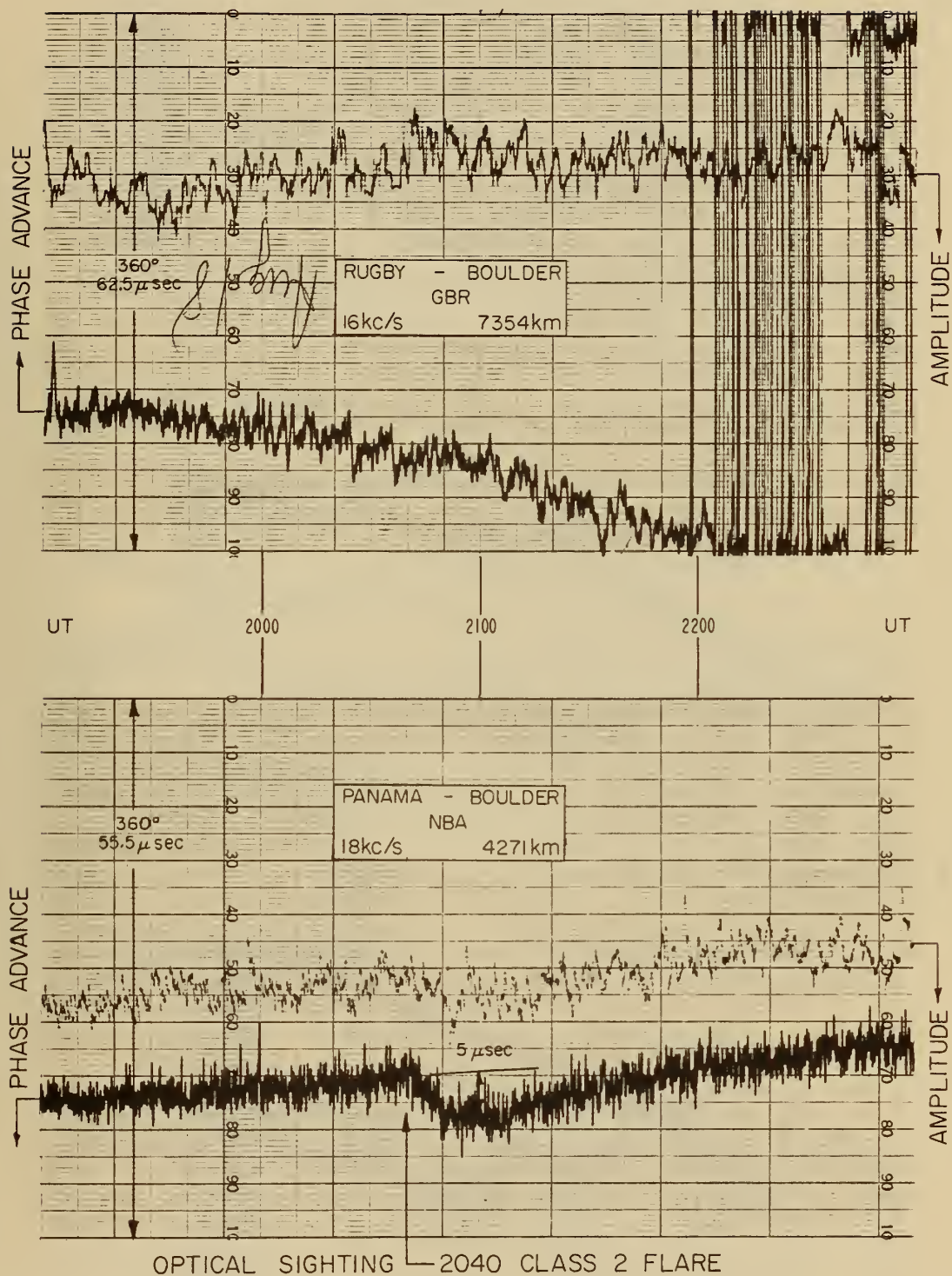


Figure 13

SUDDEN PHASE ANOMALY 1-SEPTEMBER 1961 UT

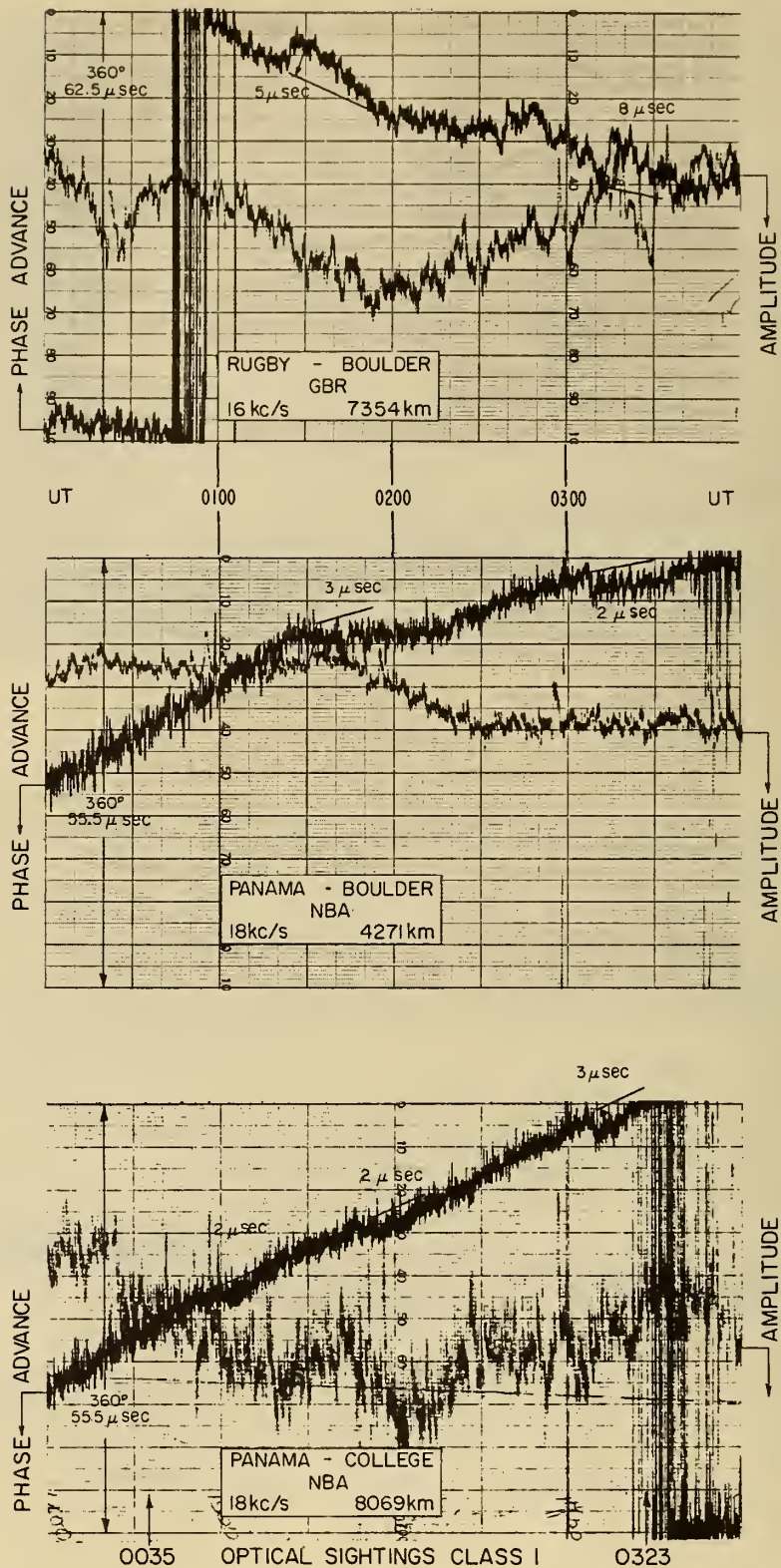


Figure 14

SUDDEN PHASE ANOMALYS 2-SEPTEMBER 1961 UT

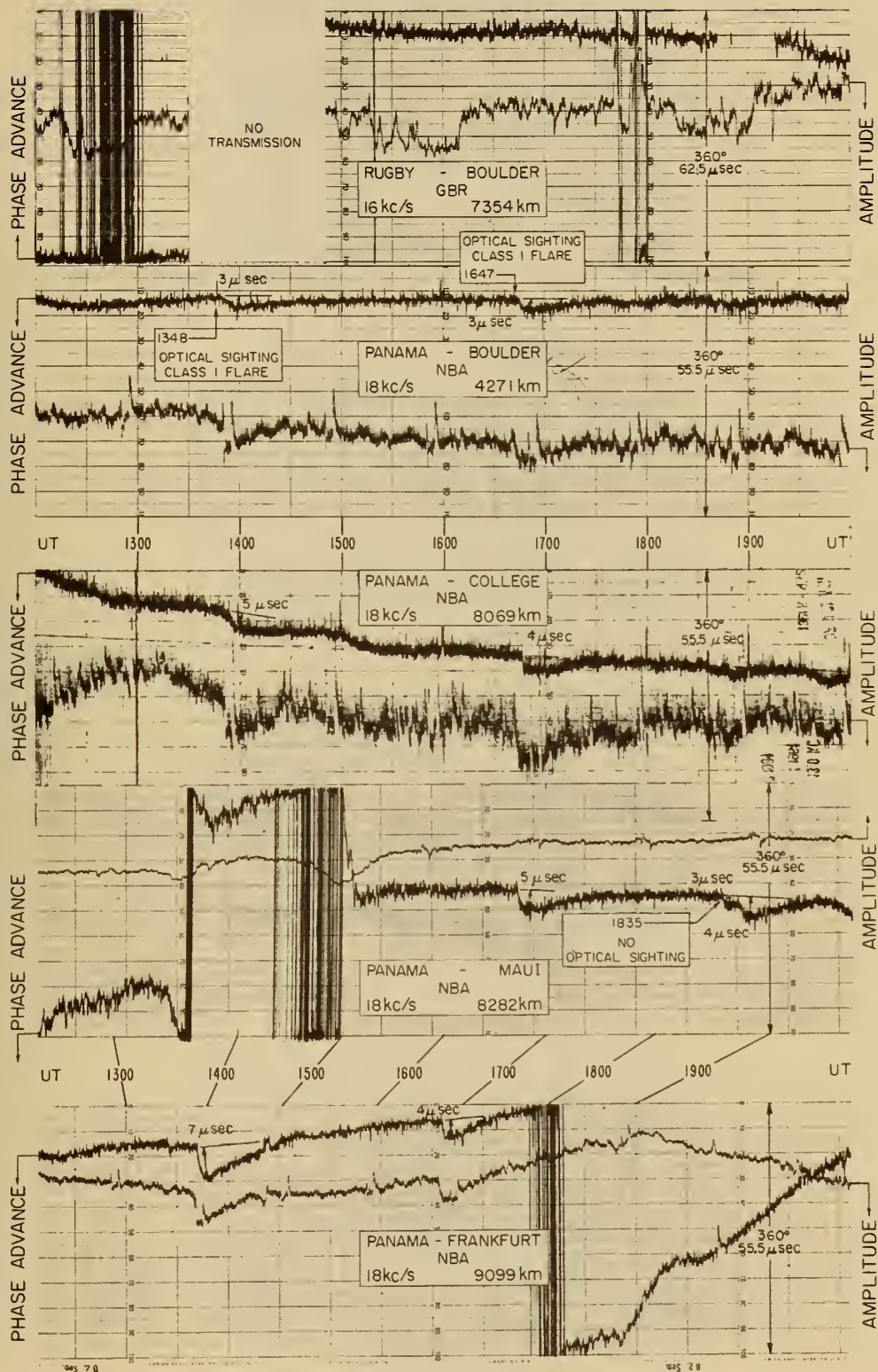


Figure 15

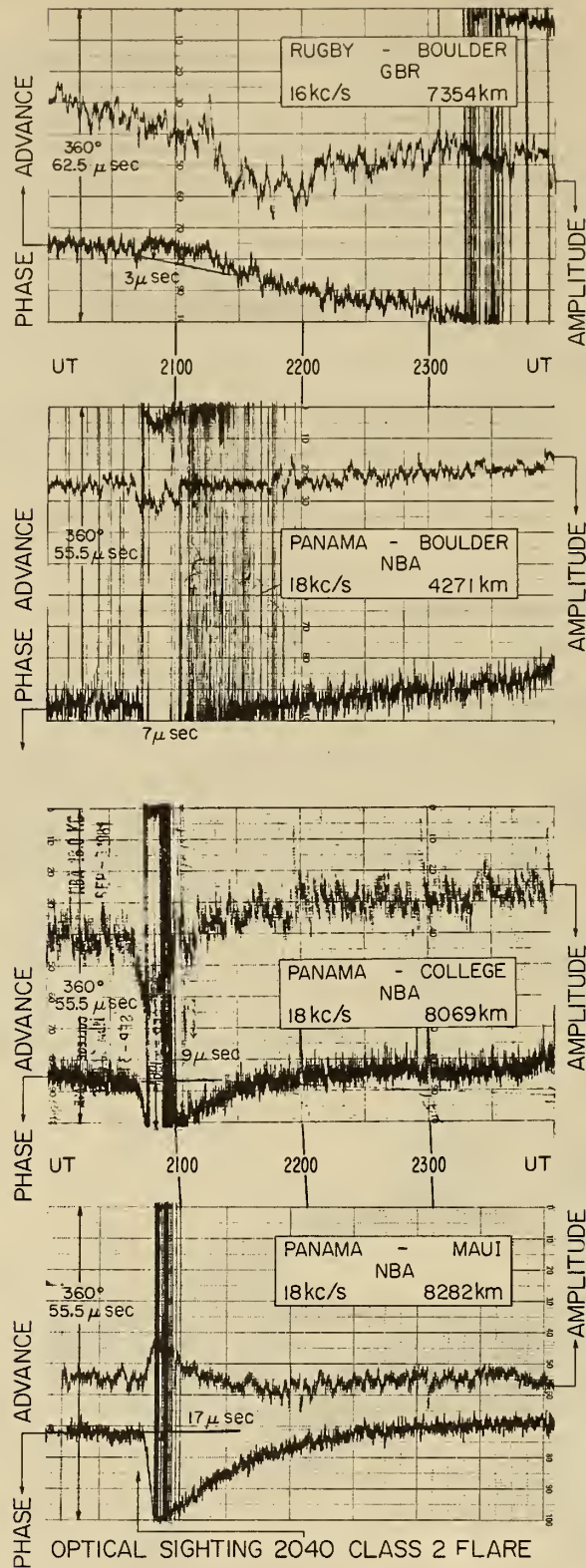


Figure 16

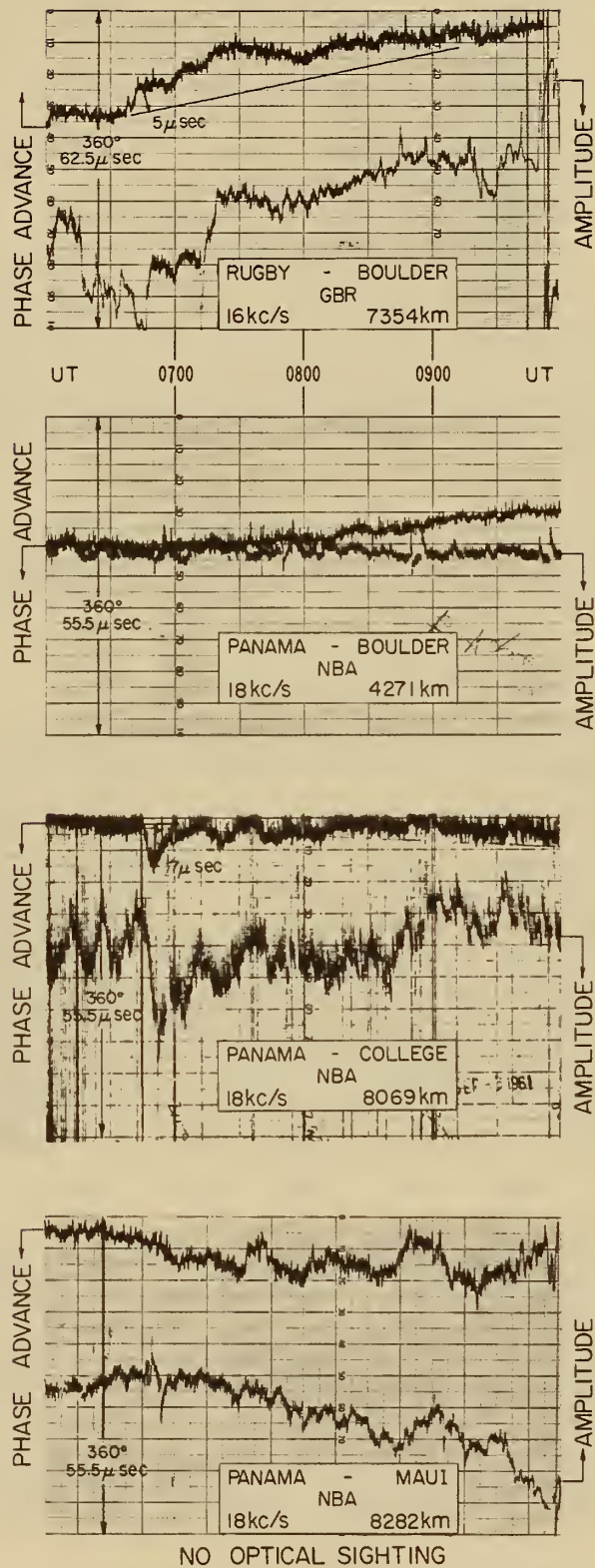
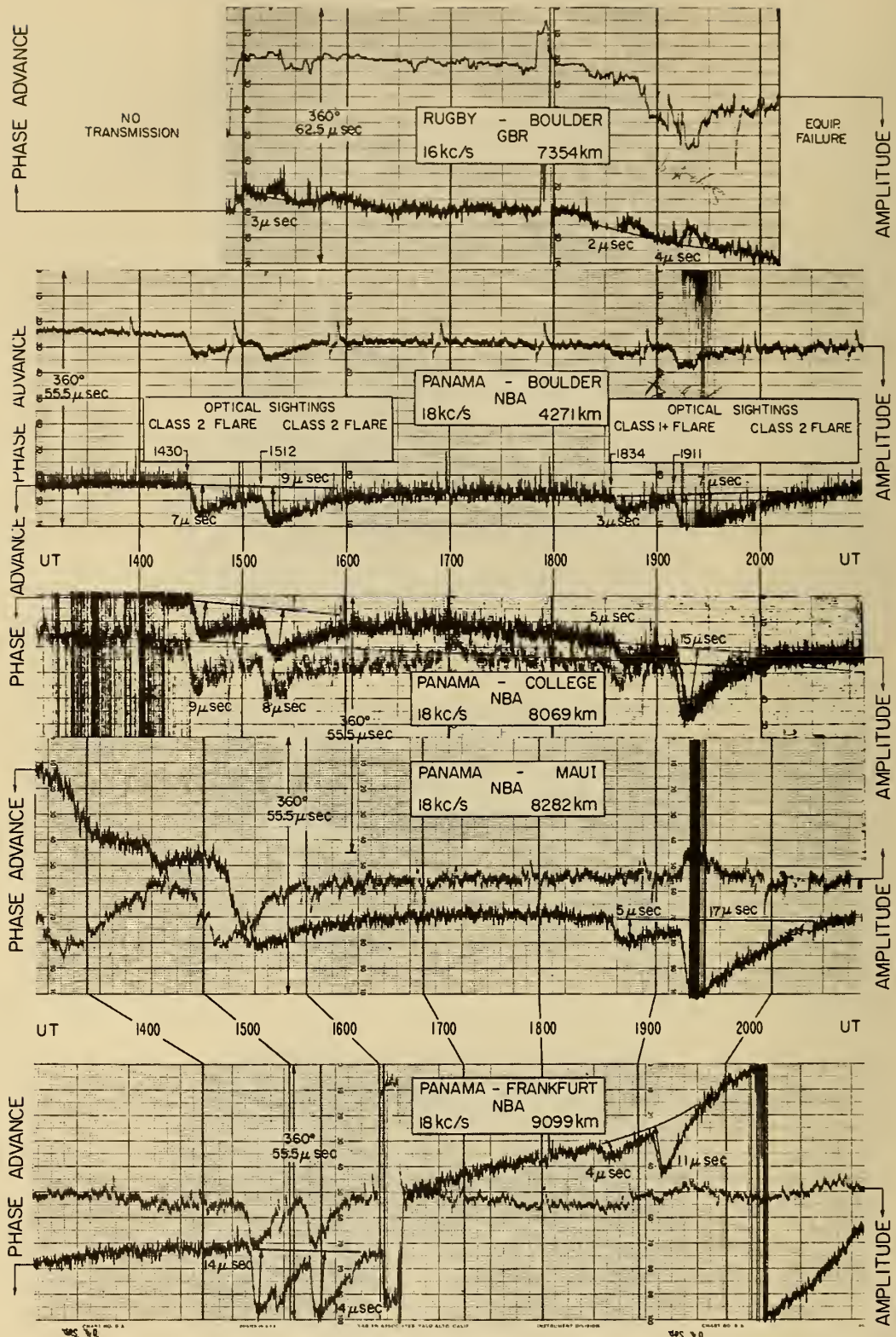


Figure 17a

SUDDEN PHASE ANOMALY 4-SEPTEMBER 1961 UT



Multiple path SPA observations of 4 solar flares which occurred on 4 September 1961 UT.

Figure 17b

SUDDEN PHASE ANOMALY 5-SEPTEMBER 1961 UT

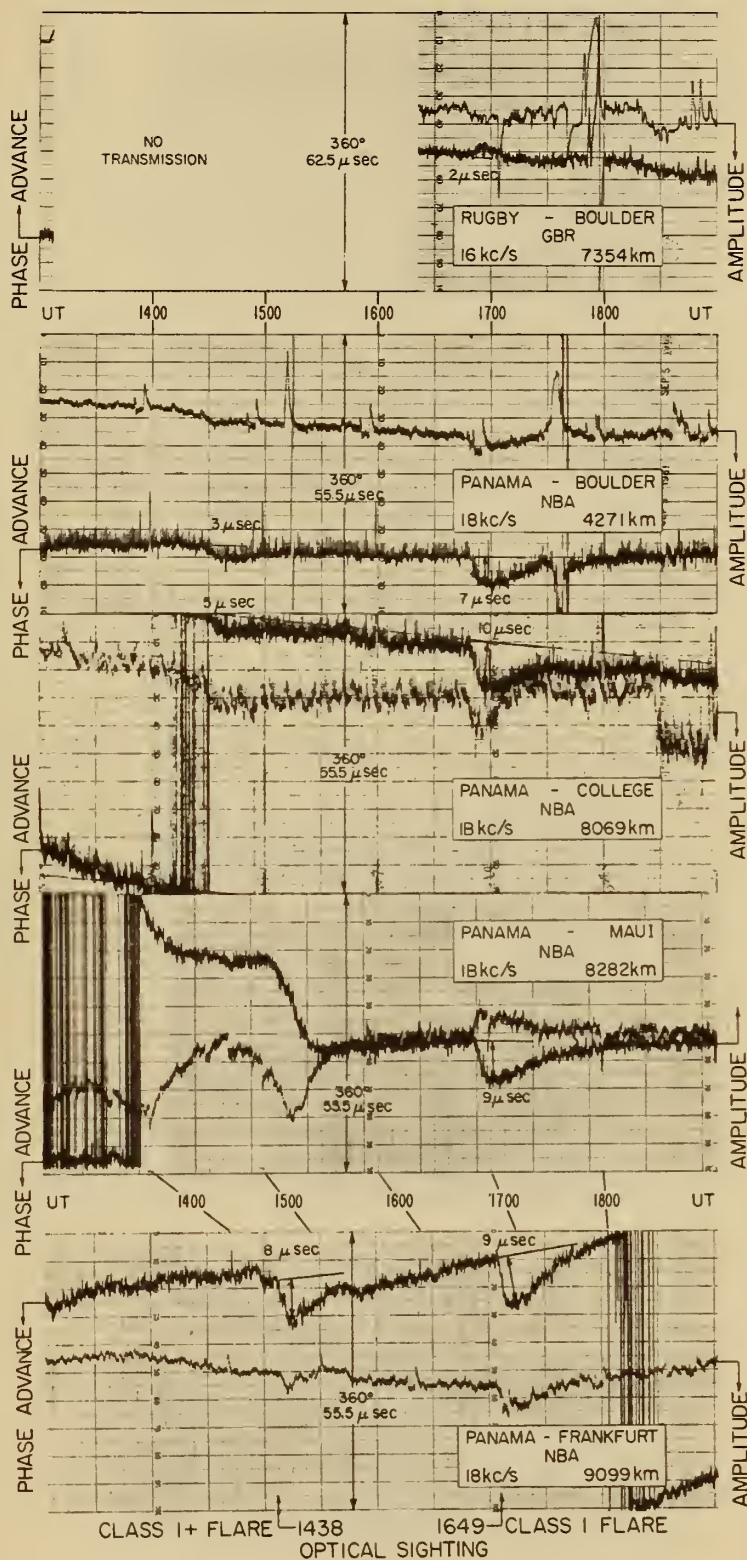


Figure 18

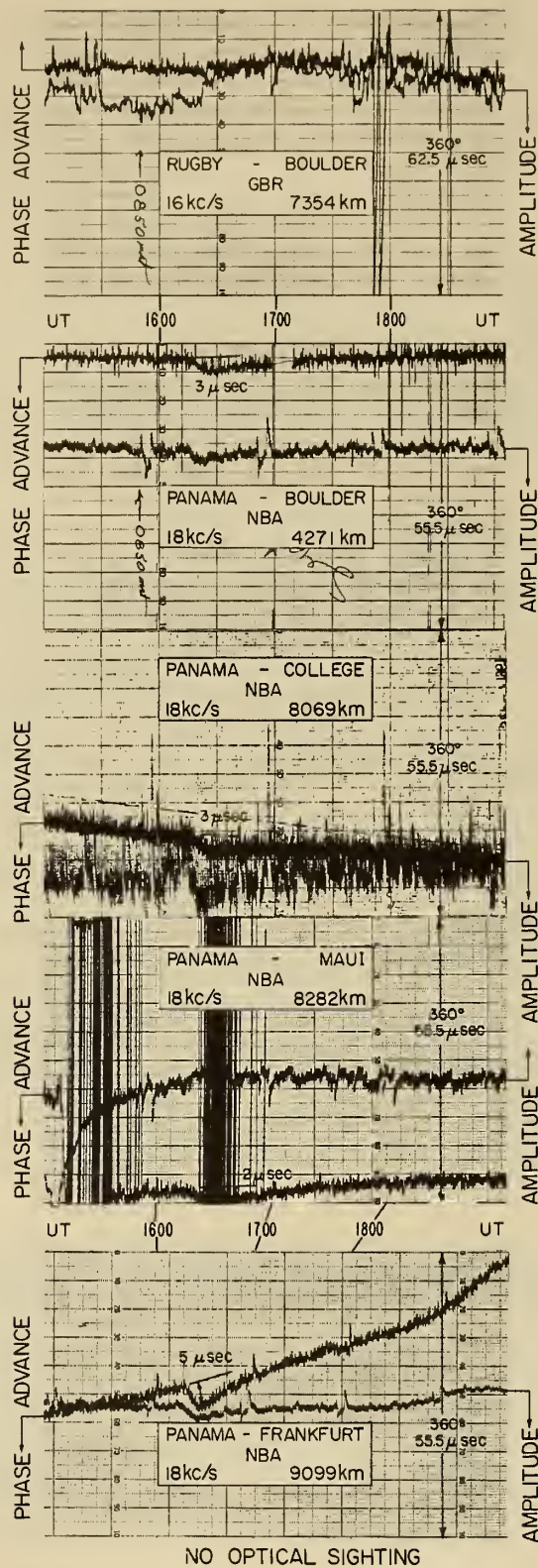


Figure 19

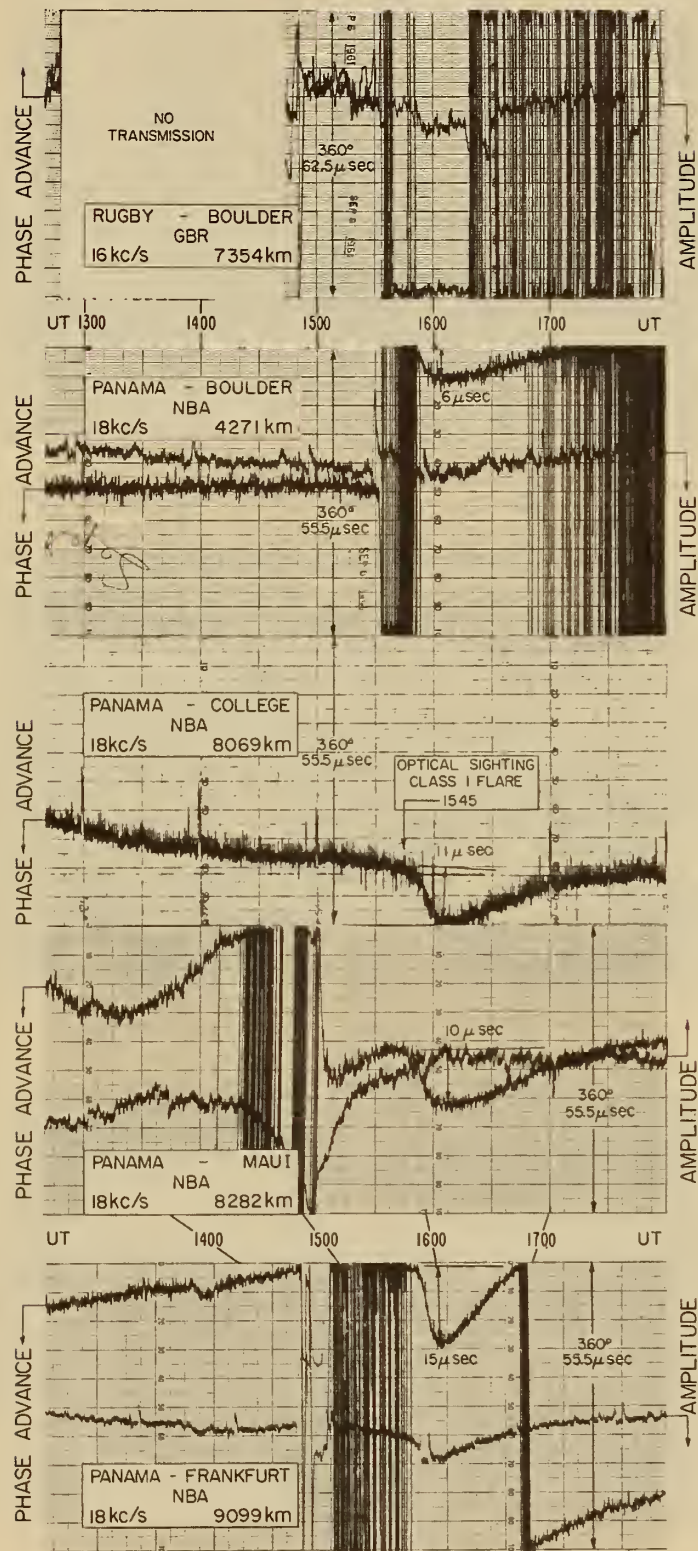


Figure 20

SUDDEN PHASE ANOMALY 5 - NOVEMBER 1961 UT

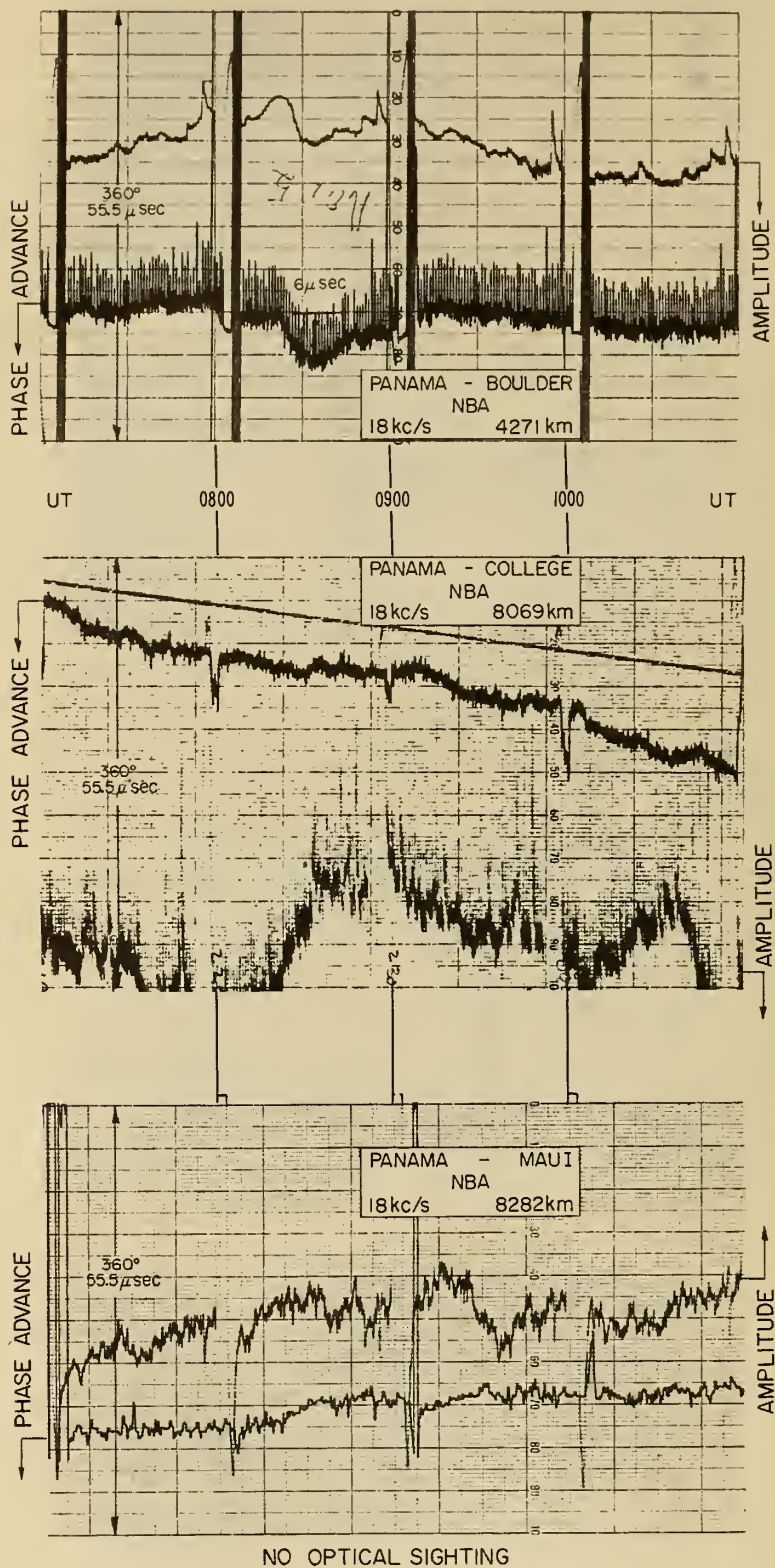


Figure 21

SUDDEN PHASE ANOMALY 10-NOVEMBER 1961 UT

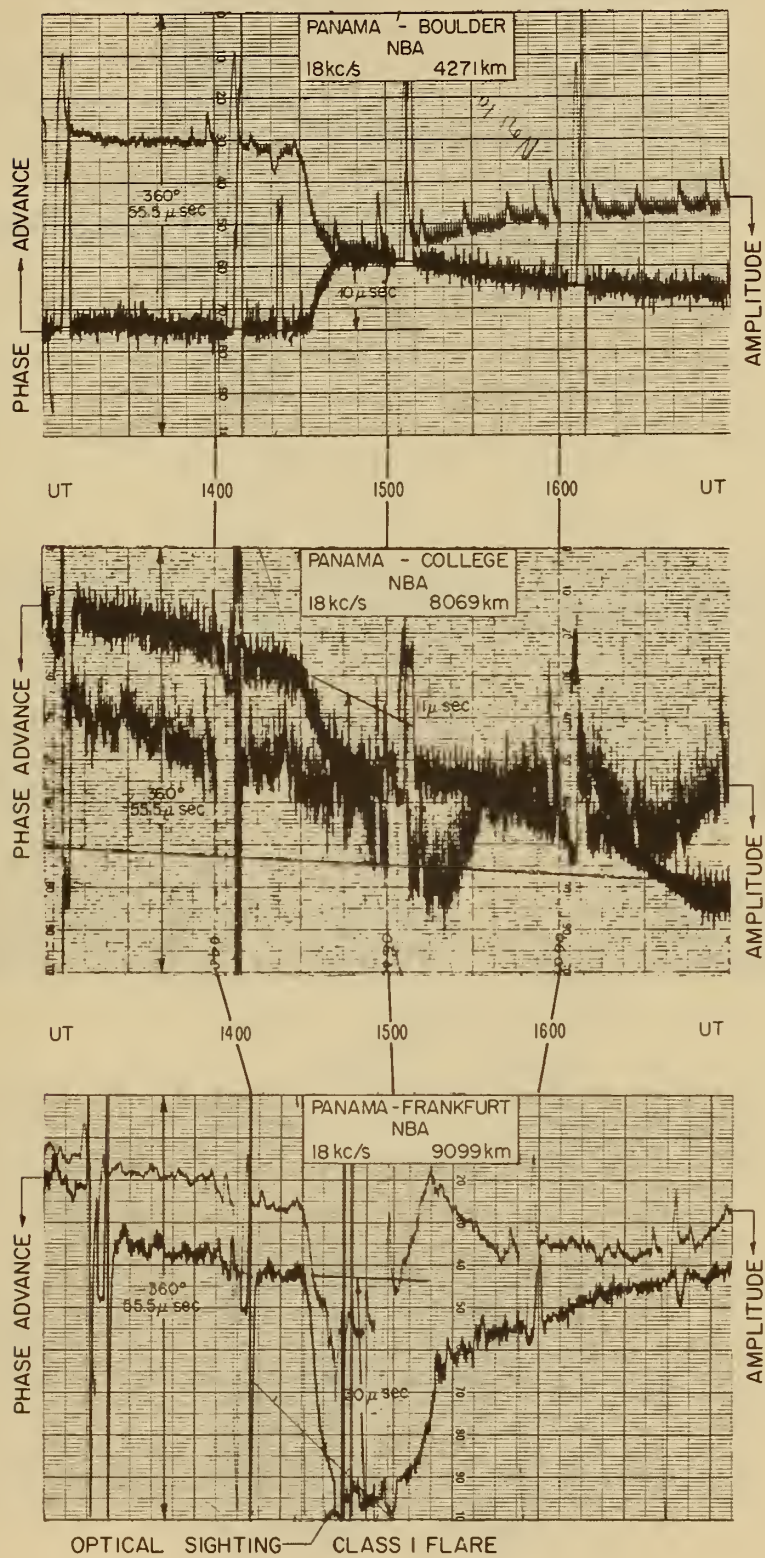


Figure 22

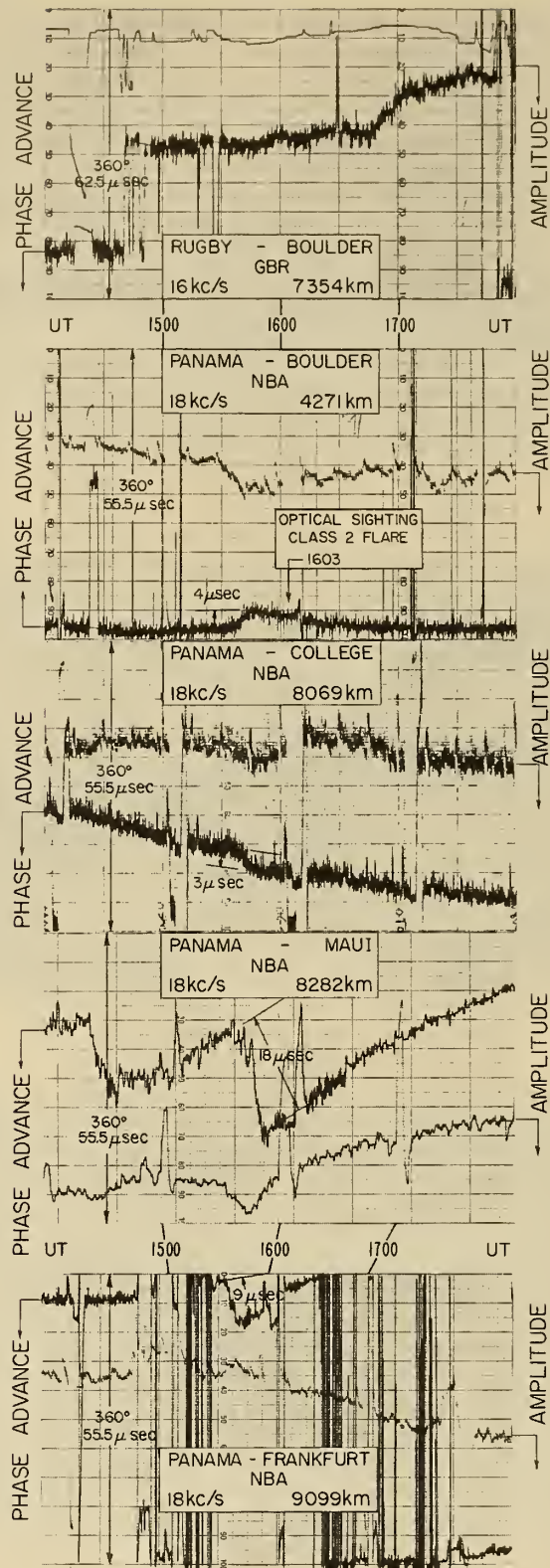
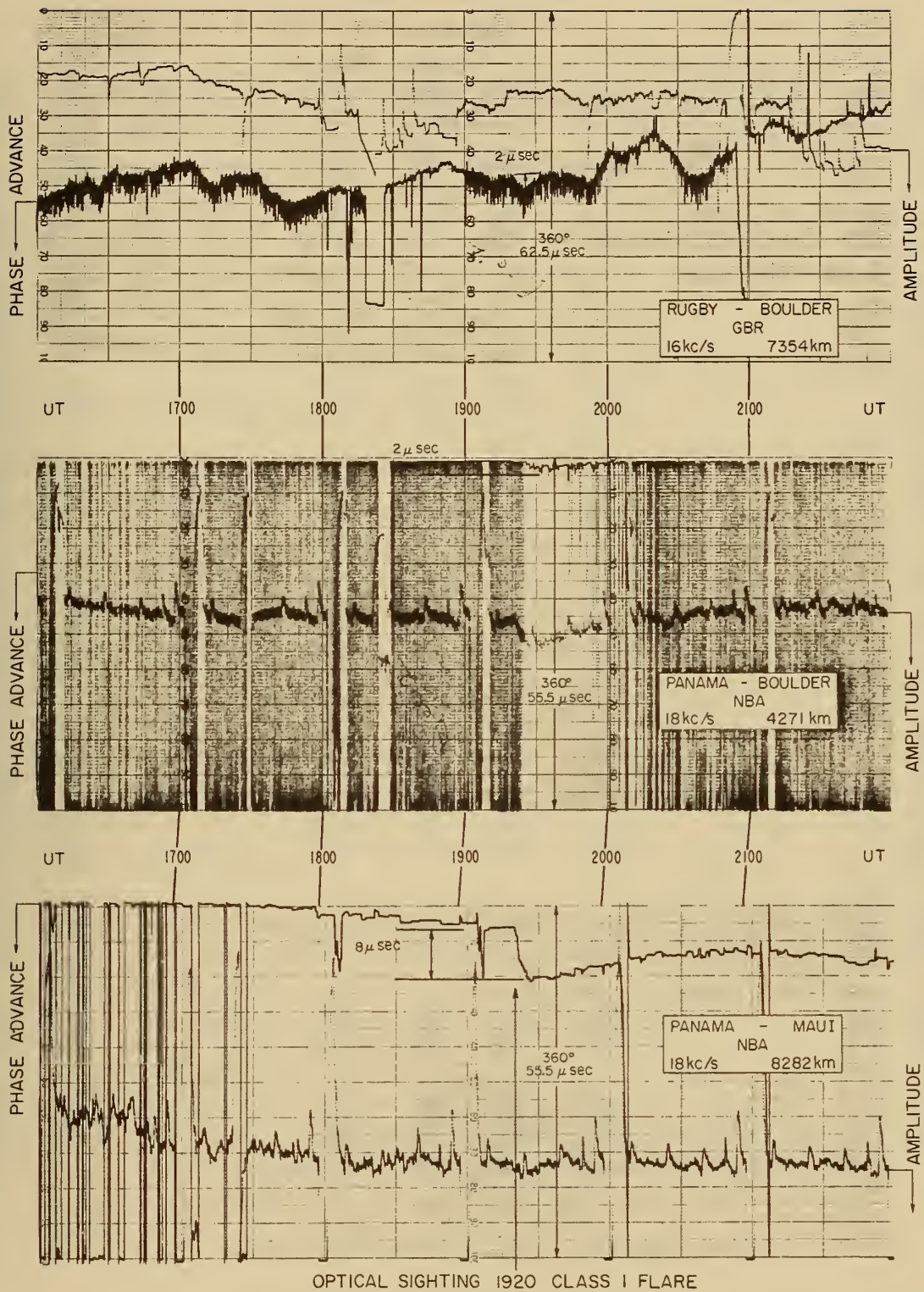


Figure 23

SUDDEN PHASE ANOMALY 2-DECEMBER 1961 UT



OPTICAL SIGHTING 1920 CLASS I FLARE

Figure 24

TABLE No. 1

| Flare Number | Date 1961 | Optical Class | Optical Sighting UT | Time of Beginning SPA (UT) | Time of Maximum SPA (UT) | End Time SPA (UT) | $\Delta \varphi$ Degrees | $\Delta \varphi$ Micro Sec | Δh Km | $\frac{d\varphi}{dt}$ Deg/Min | χ Ave. Degrees | Average Cos χ |
|--|--------------|---------------------|---------------------------|----------------------------------|--------------------------------|------------------------------|-----------------------------|-------------------------------|--------------------|----------------------------------|----------------------------------|--------------------------------------|
| 1 NBA-BO GBR-BO | 1 May | 1 | 1621 | 1623 1623 | 1630 1634 | 1852 1745 | 26 29 | 4 5 | 2.2 1.4 | 4 3 | 27.51 47.35 | .88689 .67747 |
| 2 NBA-BO GBR-BO | 5 Jun | 1 | 1523 | 1523 1523 | 1538 1534 | 1644 1650 | 39 17 | 6 3 | 3.3 0.8 | 4 2 | 38.23 41.58 | .78550 .74801 |
| 3 NBA-BO GBR-BO NBA-CO NPG-CO | 11 Jul | 1+ | 1133 | 1135 | 1142 | 1225 | 32 | 5 | 2.7 | 9 | 87.11 61.22 86.88 90.00 | .05029 .43133 .05439 0000 |
| 4 NBA-BO NBA-CO NPG-CO | 11 Jul | 1+ | 1332 | 1334 1335 | 1340 1340 | 1500 1450 | 91 39 | 14 6 | 7.6 1.7 | 12 7 | 63.35 67.81 82.00 | .44843 .37756 .13913 |
| 5 GBR-BO NBA-CO NBA-BO NPG-CO | 11 Jul | 3 | 1640 | 1636 1634 1616 1633 | 1712 1710 1710 1711 | 2000 2100 2000 2100 | 150 168 155 47 | 26 26 24 7 | 8.6 8.5 15.0 | 8 10 7 1 | 41.36 38.27 24.41 58.48 | .75050 .78501 .91058 .52268 |
| 6 NBA-BO GBR-BO | 15 Jul | 2+ | 1510 | 1511 1510 | 1517 1526 | | 26 17 | 4 3 | 2.2 0.8 | 9 2 | 42.44 43.23 | .73791 .72861 |
| 7 NBA-BO GBR-BO NBA-CO NPG-CO | 17 Jul | No Optical Sighting | | 2007 | 2015 | 2120 | 19 | 3 | 1.6 | 10 | 29.33 57.92 | .87173 .53104 |
| | | | | 1951 1950 | 2012 2012 | 2100 2112 | 19 13 | 3 2 | 0.9 | 1 2 | 34.05 37.98 | .82847 .78815 |
| 8 NBA-BO GBR-BO NBA-CO NPG-CO | 17 Jul | 1 | 2125 | 2140 2140 2140 | 2147 2210 2148 | 2330 2342 2348 | 39 29 65 | 6 5 10 | 3.3 1.4 2.8 | 40 1 14 | 49.20 63.67 46.77 37.77 | .65335 .44352 .68492 .79048 |
| 9 NBA-BO GBR-BO NBA-CO NPG-CO | 18 Jul | 2 | 0813 | | | | | | | | 90.00 72.37 90.00 90.00 | 0000 .30283 0000 0000 |
| | | | | 0813 | 0815 | | 19 | 3 | 0.9 | 13 | | |
| 10 NBA-BO GBR-BO NBA-CO NPG-CO | 18 Jul | 3 | 0945 | | | | | | | | 90.00 66.10 90.00 90.00 | 0000 .40498 0000 0000 |
| | | | | 0956 | 1006 | 1035 | 40 | 7 | 2.0 | 4 | | |
| 11 GBR-BO NBA-BO NPG-CO | 20 Jul | 3 | 1553 | 1553 1553 1553 | 1557 1600 1557 | 1950 2000 2000 | 86 110 33 | 15 17 5 | 5.0 10.6 | 30 90 30 | 42.70 34.18 65.74 | .73491 .82724 .41078 |
| 12 GBR-BO NBA-BO NBA-CO NPG-CO | 21 Jul | 2 | 1714 | | | | | | | | 43.41 19.86 35.94 56.45 | .72635 .94050 .80960 .55264 |
| | | | | 1702 1702 1703 | 1710 1710 1712 | 2000 2000 1753 | 64 78 13 | 10 12 2 | 6.2 3.9 | 42 22 1 | | |

TABLE No. 1 (page 2)

| Flare Number | Date 1961 | Optical Class | Optical Sighting UT | Time of Beginning SPA (UT) | Time of Maximum SPA (UT) | End Time SPA (UT) | $\Delta \varphi$ Degrees | $\Delta \varphi$ Micro Sec | Δh Km | $\frac{d\varphi}{dt}$ Deg/Min | χ Ave. Degrees | Average Cos χ |
|--|--------------|---------------------|---------------------------|----------------------------------|--------------------------------|------------------------------|-----------------------------|-------------------------------|--------------------------|----------------------------------|---|--|
| 13 NBA-CO NPG-CO | 23 Jul | No Optical Sighting | | 0803 0804 | 0815 0813 | 0842 0900 | 19 40 | 3 6 | 0.9 | 3 5 | 90.00 90.00 | 0000 0000 |
| 14 NBA-BO NBA-CO NPG-CO | 24 Jul | 3 | 1722 | 1750 1730 | 1815 1820 | 1930 1950 | 26 32 | 4 5 | 2.2 1.4 | 1 1 | 13.44 31.80 51.06 | .97261 .84985 .62845 |
| 15 NBA-BO GBR-BO | 15 Aug | 1 | 1645 | 1645 | 1655 | 1750 | 13 | 2 | 1.1 | 2 | 25.12 48.65 | .90540 .66053 |
| 16 NBA-BO GBR-BO | 18 Aug | 2 | 2040 | 2040 | 2100 | 2210 | 32 | 5 | 2.7 | 2 | 39.36 62.90 | .77316 .45542 |
| 17 NBA-BO GBR-BO NBA-CO | 1 Sep | No Optical Sighting | | 0130 0125 | 0140 0130 | 0200 | 19 29 | 3 5 | 1.6 1.4 | 1 3 | 89.35 89.17 78.23 | .01133 .01441 .20384 |
| 18 NBA-BO GBR-BO NBA-CO | 1 Sep | No Optical Sighting | | | | | | | | | 90.00 90.00 78.84 | 0000 0000 .19343 |
| 19 NBA-BO GBR-BO NBA-CO | 1 Sep | 1 | 0323 | 0307 0310 0308 | 0318 0312 0315 | 0352 0350 0346 | 52 12 19 | 8 2 3 | 4.3 0.6 0.9 | 1 10 2 | 90.00 90.00 83.41 | 0000 0000 .11463 |
| 20 NBA-BO GBR-BO NBA-CO NBA-MA NBA-FK | 2 Sep | 1 | 1348 | 1350 1350 1351 | 1400 1400 1400 | 1500 1500 1500 | 19 32 45 | 3 5 7 | 1.6 1.4 1.8 | 2 3 23 | 65.79 60.65 71.00 72.02 42.42 | .40943 .49006 .32544 .30855 .73817 |
| 21 NBA-BO GBR-BO NBA-CO NBA-MA NBA-FK | 2 Sep | 1 | 1647 | 1646 1646 1645 1646 | 1651 1651 1651 1652 | 1730 1730 1735 1731 | 19 26 32 26 | 3 4 5 4 | 1.6 1.2 1.4 1.0 | 2 14 14 11 | 28.12 54.22 45.91 49.79 42.95 | .88191 .58454 .69573 .64553 .73187 |
| 22 NBA-BO GBR-BO NBA-CO NBA-MA NBA-FK | 2 Sep | No Optical Sighting | | | | | | | | | 21.86 60.08 39.15 30.06 55.49 | .92806 .49878 .77545 .86544 .56649 |
| 23 NBA-BO GBR-BO NBA-CO NBA-MA NBA-FK | 2 Sep | No Optical Sighting | | | | | | | | | 22.52 60.74 39.17 28.98 56.39 | .92369 .48875 .77527 .87473 .55347 |
| 24 GBR-BO NBA-BO NBA-CO NBA-MA | 3 Sep | 2 | 2040 | 2043 2043 2041 2043 | 2050 2051 2050 2051 | 2130 2130 2242 2227 | 17 45 58 110 | 3 7 9 17 | 1.0 1.3 3.3 5.4 | 5 4 14 21 | 65.01 43.16 48.18 27.68 | .42240 .72943 .66672 .88548 |

TABLE No. 1 (page 3)

| Flare Number | Date 1961 | Optical Class | Optical Sighting UT | Time of Beginning SPA (UT) | Time of Maximum SPA (UT) | End Time SPA (UT) | $\Delta \phi$ Degrees | $\Delta \phi$ Micro Sec | Δh Km | $\frac{d\phi}{dt}$ Deg/Min | χ Ave. Degrees | Average Cos χ |
|-----------------|--------------|---------------------|---------------------------|----------------------------------|--------------------------------|----------------------|--------------------------|----------------------------|------------------|-------------------------------|------------------------|-----------------------|
| 25 | 4 Sep | No Optical Sighting | | | | | | | | | | |
| NBA-BO | | | | | | | | | | | 90.00 | 0000 |
| GBR-BO | | | | 0637 | 0645 | | 29 | 5 | 1.4 | 9 | 84.52 | .09538 |
| NBA-CO | | | | 0645 | 0650 | | 45 | 7 | 2.0 | 13 | 90.00 | 0000 |
| NBA-MA | | | | | | | | | | | 90.00 | 0000 |
| 26 | 4 Sep | 2 | 1430 | | | | | | | | | |
| NBA-BO | | | | 1429 | 1437 | | 45 | 7 | 3.8 | 10 | 54.59 | .57940 |
| NBA-CO | | | | 1431 | 1436 | | 58 | 9 | 2.6 | 24 | 64.55 | .42972 |
| NBA-MA | | | | | | | | | | | 66.06 | .40576 |
| NBA-FK | | | | 1430 | 1438 | | 91 | 14 | 3.6 | 23 | 38.98 | .77731 |
| 27 | 4 Sep | 2 | 1512 | | | | | | | | | |
| NBA-BO | | | | 1510 | 1518 | 1650 | 58 | 9 | 4.9 | 16 | 45.88 | .69612 |
| GBR-BO | | | | 1510 | 1518 | 1532 | 17 | 3 | 0.9 | 2 | 55.54 | .56575 |
| NBA-CO | | | | 1512 | 1520 | 1641 | 52 | 8 | 2.3 | 10 | 58.97 | .51538 |
| NBA-MA | | | | | | | | | | | 61.72 | .47364 |
| NBA-FK | | | | 1514 | 1520 | 1615 | 91 | 14 | 3.6 | 25 | 38.12 | .78661 |
| 28 | 4 Sep | 1 | 1834 | | | | | | | | | |
| GBR-BO | | | | 1833 | 1843 | 1900 | 11 | 2 | 1.0 | 1 | 61.01 | .48463 |
| NBA-BO | | | | 1831 | 1841 | | 19 | 3 | 1.8 | 5 | 22.73 | .92233 |
| NBA-CO | | | | 1837 | 1844 | | 32 | 5 | 1.6 | 5 | 39.75 | .76878 |
| NBA-MA | | | | 1837 | 1846 | | 32 | 5 | 1.9 | 27 | 29.84 | .86740 |
| NBA-FK | | | | 1836 | 1845 | | 25 | 4 | 1.1 | 3 | 56.08 | .55803 |
| 29 | 4 Sep | 2 | 1911 | | | | | | | | | |
| GBR-BO | | | | 1910 | 1919 | 1940 | 23 | 4 | 1.3 | 4 | 61.60 | .47560 |
| NBA-BO | | | | 1910 | 1917 | 2045 | 45 | 7 | 5.0 | 10 | 26.85 | .89219 |
| NBA-CO | | | | 1912 | 1919 | 2020 | 97 | 15 | 4.6 | 18 | 40.56 | .75964 |
| NBA-MA | | | | 1913 | 1921 | 2027 | 110 | 17 | 5.4 | 18 | 25.96 | .89908 |
| NBA-FK | | | | 1910 | 1917 | 1943 | 71 | 11 | 2.4 | 12 | 59.32 | .51016 |
| 30 | 5 Sep | 1+ | 1438 | | | | | | | | | |
| NBA-BO | | | | 1430 | 1440 | 1510 | 19 | 3 | 1.6 | 2 | 54.68 | .57807 |
| NBA-CO | | | | 1430 | 1440 | 1520 | 32 | 5 | 1.4 | 3 | 64.38 | .43239 |
| NBA-MA | | | | | | | | | | | 66.07 | .40548 |
| NBA-FK | | | | 1439 | 1446 | 1520 | 52 | 8 | 2.0 | 6 | 39.25 | .77432 |
| 31 | 5 Sep | 1 | 1649 | | | | | | | | | |
| NBA-BO | | | | 1650 | 1657 | 1800 | 45 | 7 | 3.8 | 7 | 27.64 | .88582 |
| GBR-BO | | | | 1650 | 1657 | 1710 | 12 | 2 | 0.6 | 2 | 55.43 | .56734 |
| NBA-CO | | | | 1650 | 1656 | 1825 | 65 | 10 | 2.9 | 10 | 45.88 | .69614 |
| NBA-MA | | | | 1651 | 1702 | 1823 | 58 | 9 | 2.5 | 10 | 48.49 | .66263 |
| NBA-FK | | | | 1649 | 1700 | 1810 | 58 | 9 | 2.3 | 14 | 44.58 | .71225 |
| 32 | 7 Sep | No Optical Sighting | | | | | | | | | | |
| GBR-BO | | | | | | | | | | | 55.57 | .56542 |
| NBA-BO | | | | 1618 | 1628 | 1730 | 19 | 3 | 1.8 | 2 | 33.39 | .83491 |
| NBA-CO | | | | 1618 | 1628 | 1730 | 19 | 3 | 0.9 | 2 | 50.17 | .64038 |
| NBA-MA | | | | 1620 | 1632 | 1722 | 13 | 2 | 0.6 | 1 | 55.39 | .56795 |
| NBA-FK | | | | 1620 | 1626 | 1729 | 32 | 5 | 1.4 | 4 | 41.97 | .74347 |
| 33 | 8 Sep | 1 | 1545 | | | | | | | | | |
| GBR-BO | | | | | | | | | | | 55.96 | .55973 |
| NBA-BO | | | | 1531 | 1603 | 1730 | 39 | 6 | 4.3 | 6 | 38.53 | .78227 |
| NBA-CO | | | | 1551 | 1605 | 1723 | 71 | 11 | 3.6 | 6 | 53.99 | .58789 |
| NBA-MA | | | | 1547 | 1611 | 1745 | 65 | 10 | 3.2 | 8 | 57.88 | .53155 |
| NBA-FK | | | | 1542 | 1602 | 1742 | 97 | 15 | 4.4 | 12 | 40.44 | .76102 |
| 34 | 5 Nov | No Optical Sighting | | | | | | | | | | |
| NBA-BO | | | | 0822 | 0833 | 0920 | 39 | 6 | 3.3 | 4 | 90.00 | 0000 |
| NBA-CO | | | | | | | | | | | 90.00 | 0000 |
| NBA-MA | | | | | | | | | | | 90.00 | 0000 |

TABLE No. 1 (page 4)

| Flare Number | Date 1961 | Optical Class | Optical Sighting UT | Time of Beginning SPA (UT) | Time of Maximum SPA (UT) | End Time SPA (UT) | $\Delta \varphi$ Degrees | $\Delta \varphi$ Micro Sec | Δh Km | $\frac{d\varphi}{dt}$ Deg/Min | χ Ave. Degrees | Average Cos χ |
|-----------------|--------------|------------------|---------------------------|----------------------------------|--------------------------------|----------------------|-----------------------------|-------------------------------|------------------|----------------------------------|------------------------|-----------------------|
| 35 | 10 Nov | 1 | 1434 | | | | | | | | | |
| NBA-BO | | | | 1434 | 1449 | 1700 | 65 | 10 | 6.2 | 8 | 65.05 | .42169 |
| NBA-CO | | | | 1434 | 1446 | 1543 | 71 | 11 | 3.6 | 7 | 68.35 | .36878 |
| NBA-FK | | | | 1423 | 1438 | 1700 | 194 | 30 | 9.3 | 28 | 58.62 | .52059 |
| 36 | 16 Nov | 2 | 1603 | | | | | | | | | |
| NBA-BO | | | | 1533 | 1550 | 1650 | 26 | 4 | 2.2 | 3 | 55.39 | .56793 |
| GBR-BO | | | | | | | | | | | 78.65 | .19674 |
| NBA-CO | | | | 1537 | 1550 | 1632 | 19 | 3 | 0.9 | 3 | 63.47 | .44663 |
| NBA-MA | | | | 1538 | 1552 | 1640 | 117 | 18 | 5.0 | 22 | 63.35 | .44849 |
| NBA-FK | | | | 1536 | 1549 | 1638 | 58 | 9 | 2.3 | 8 | 60.21 | .49670 |
| 37 | 2 Dec | 1 | 1920 | | | | | | | | | |
| GBR-BO | | | | 1921 | 1926 | 1933 | 11 | 2 | 0.6 | 4 | 75.92 | .24320 |
| NBA-BO | | | | 1923 | 1932 | 1950 | 19 | 3 | 1.8 | 1 | 52.85 | .60377 |
| NBA-MA | | | | 1924 | 1930 | 1956 | 52 | 8 | 2.5 | 26 | 45.49 | .70094 |

Table 2

Distribution of maximum phase shift $\Delta\phi$, with optical flare classification

| Optical flare classification | 1 | 2 | 3 |
|--|----|-----|-----|
| maximum $\Delta\phi$ (in degrees) | 30 | 18 | 28 |
| mean $\Delta\phi$ (in degrees) | 7 | 8 | 14 |
| minimum $\Delta\phi$ (in degrees) | 2 | 2 | 4 |
| Value of $\Delta\phi$ exceeded 25% of time | 9° | 12° | 24° |
| Value of $\Delta\phi$ exceeded 50% of time | 5° | 7° | 7° |
| Value of $\Delta\phi$ exceeded 75% of time | 3° | 3° | 5° |

Table 3
Distribution of maximum rates of change of phase ($d\phi/dt$) with
optical flare classification

| Optical flare classification | 1 | 2 | 3 | |
|---|----|----|----|--------------|
| maximum $d\phi/dt$ | 40 | 42 | 90 | degrees/min. |
| mean $d\phi/dt$ | 9 | 13 | 18 | degrees/min. |
| minimum $d\phi/dt$ | 1 | 1 | 1 | degrees/min. |
| Values of $d\phi/dt$ exceeded 25% of time | 10 | 21 | 30 | degrees/min. |
| Values of $d\phi/dt$ exceeded 50% of time | 6 | 10 | 7 | degrees/min. |
| Values of $d\phi/dt$ exceeded 75% of time | 2 | 4 | 1 | degrees/min. |





